

February 16, 1995

LBL-36659  
UCB-PTH-95/01  
nucl-th/9502037

## Tables of $SU(3)$ Isoscalar Factors\*

Thomas A. Kaeding<sup>†</sup>

*Theoretical Physics Group  
Lawrence Berkeley Laboratory  
University of California  
Berkeley, California 94720*

### Abstract

The Clebsch-Gordan coefficients of  $SU(3)$  are useful in calculations involving baryons and mesons, as well as in calculations involving arbitrary numbers of quarks. For the latter case, one needs the coupling constants between states of nonintegral hypercharges. The existing published tables are insufficient for many such applications, and therefore we have compiled this collection. This report supplies the isoscalar factors required to reconstruct the Clebsch-Gordan coefficients for a large set of products of representations.

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\*This work was supported by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U.S. Department of Energy under Contract DE-AC03-76SF00098.

<sup>†</sup>Electronic address: `kaedin@theorm.lbl.gov`.

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Tables of  $SU(3)$  Clebsch-Gordan coefficients and their isoscalar factors<sup>1</sup> have been compiled in the past [1] [2] [3] [4] [5], and programs have been distributed that calculate these coefficients [6] [7] [8]. However, for calculations involving large or arbitrary numbers of quarks, having additional tables is convenient. For this purpose the present work extends the available set of tables of coefficients. Because the tables of Clebsch-Gordan coefficients would occupy far too much space, we have extracted the isoscalar factors and present them here. Anyone wishing a good theoretical background is suggested to consult [1] [9] [10] [11].

A few things must be discussed. Our phase conventions are explained in Section 1. In Section 2 we show the notation of the tables and explain how to reconstruct the Clebsch-Gordan coefficients from the isoscalar factors. There we also present some symmetry relations that allow us to omit some tables. Finally, the tables themselves are presented.

The tables of Clebsch-Gordan tables that were reduced to the present set of isoscalar tables were generated by computer. Most of the routines are described in [12]. Because we take the simple-minded approach of explicitly constructing the representations, and use integers for exact precision, the main limitations of the routines are due to memory allocation and integer overflows. Any omissions in the set of isoscalar tables should be attributed to our lack of computing power.

## 1 Conventions

The representations of  $SU(3)$  can be thought of as consisting of  $SU(2)$  multiplets (henceforth called isomultiplets), each at a specific hypercharge. We have adopted the Condon-Shortley phase convention [13] for these isomultiplets. This means that the eigenvalues of the isospin-raising and -lowering operators (the  $T$ -spin operators) are real and positive. What remains is to specify the relative phases between the isomultiplets of a given representation and the overall phases of representations in the Clebsch-Gordan series.

For the relative phases between isomultiplets in a given representation, we have adopted the de Swart phase convention [1]. It corresponds to requiring that the eigenvalues of the  $V$ -spin operators be real and positive. This is simply an extension of the Condon-Shortley convention to the  $V$ -spin operators. (Recall that in flavor  $SU(3)$  the  $V$ -spin operators interchange  $u$  and  $s$  quarks.) It is not possible to simultaneously require that the eigenvalues of all operators be positive.

In a few cases, there is an arbitrary choice in the construction of representations that are multiply degenerate. By this we mean that two or more of the same representation occur in the same Clebsch-Gordan series. In these cases, we follow the prescription of [7].

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<sup>1</sup>The Clebsch-Gordan coefficients are also called *vector coupling coefficients* or *Wigner coefficients* in the literature; the isoscalar factors are also called *Racah coefficients*.

The highest outer degeneracy in this work is two, and is only present when one of the factors is an octet. The prescription of [7] corresponds to constructing the representations in the product so that the highest-isospin state of only one of them couples to the isospin-1 multiplet in the factor octet.

It remains to specify the overall phases of representations in the decomposition of the product of two irreducible representations. Representations are named as in [14], with the addition of **80** = (7, 1), **81** = (5, 2), and **90** = (4, 3) in the usual  $(p, q)$  notation. Throughout this work,  $Y$  and  $y$  denote hypercharge,  $I$  and  $i$  denote isospin. We choose to follow the phase convention of de Swart [1]. For each representation  $\mathbf{R}$  in the product, consider the state with highest third component of isospin. Call this state the state of highest weight, and call its quantum numbers  $Y_h$ ,  $I_h$ , and  $i_{h3}$ . Next consider the state in the first factor representation  $(\mathbf{r})$  that has highest isospin and couples to the highest-weight state of the product representation; call its quantum numbers  $y_h$ ,  $i_h$ , and  $i_{h3}$ . Now consider the state in the second factor representation  $(\mathbf{r}')$  with highest isospin that couples the above two states; its quantum numbers are labelled  $y'_h$ ,  $i'_h$ , and  $i'_{h3}$ . The phase convention requires that the Clebsch-Gordan coefficient between these three states be positive (and real):

$$\langle \mathbf{R} Y_h I_h i_{h3} | \mathbf{r} y_h i_h i_{h3} \mathbf{r}' y'_h i'_h i'_{h3} \rangle > 0. \quad (1)$$

With these phase conventions, the Clebsch-Gordan coefficients and isoscalar factors are real.

## 2 Reconstruction of Clebsch-Gordan Coefficients from Isoscalar Factors

The isoscalar factors depend of the identity of the representations, and on the hypercharges and isospins of the isomultiplets that are coupled. We will denote them by  $F(\mathbf{R}, Y, I; \mathbf{r}, y, i, \mathbf{r}', y', i')$ . The  $SU(3)$  Clebsch-Gordan coefficients are found as products of isoscalar factors and  $SU(2)$  Clebsch-Gordan coefficients:

$$\langle \mathbf{R} Y I I_3 | \mathbf{r} y i i_3 \mathbf{r}' y' i' i'_3 \rangle = F(\mathbf{R}, Y, I; \mathbf{r}, y, i, \mathbf{r}', y', i') \times \langle I I_3 | i i_3 i' i'_3 \rangle. \quad (2)$$

The  $SU(2)$  tables can be reconstructed from Tables  $1^3$ ,  $2^3$ ,  $3^3$ , and  $4^3$  of [13]. For isospin less than or equal to two, they can conveniently be found in the *Review of Particle Properties* [15]. Note the easily overlooked relation

$$\langle I I_3 | i i_3 i' i'_3 \rangle = (-1)^{I-i-i'} \langle I I_3 | i' i'_3 i i_3 \rangle. \quad (3)$$

There are two symmetry relations among the isoscalar factors that will allow us to omit many tables from our exposition. Those tables can be reconstructed from those that are present, with the help of the phase factors involved in these symmetry relations. Both

relations come from [1], but we rewrite them in our notation.<sup>2</sup> The first involves the order of the factor representations. If the order is reversed, then a phase  $\xi$  may enter:

$$F(\mathbf{R}, Y, I; \mathbf{r}', y', i', \mathbf{r}, y, i) = (-1)^{I-i-i'} \xi(\mathbf{R}; \mathbf{r}, \mathbf{r}') F(\mathbf{R}, Y, I; \mathbf{r}, y, i, \mathbf{r}', y', i'). \quad (4)$$

The factor  $(-1)^{I-i-i'}$  comes from Equation 3. The phase  $\xi(\mathbf{R}; \mathbf{r}, \mathbf{r}')$  does not depend on the quantum numbers of the states, but only on the identity of the representations  $\mathbf{r}$ ,  $\mathbf{r}'$ , and  $\mathbf{R}$ , and on the phase conventions described in the previous section. The second symmetry relation involves the conjugation of the representations:

$$F(\overline{\mathbf{R}}, Y, I; \overline{\mathbf{r}}, y, i, \overline{\mathbf{r}'}, y', i') = (-1)^{I-i-i'} \zeta(\mathbf{R}; \mathbf{r}, \mathbf{r}') F(\mathbf{R}, -Y, I; \mathbf{r}, -y, i, \mathbf{r}', -y', i'). \quad (5)$$

Here  $\zeta(\mathbf{R}; \mathbf{r}, \mathbf{r}')$  also does not depend on the quantum numbers of the states involved, but only on the identities of the representations and on our phase conventions. For these relations, we naturally define  $\overline{\mathbf{1}} \equiv \mathbf{1}$ ,  $\overline{\mathbf{8}} \equiv \mathbf{8}$ ,  $\overline{\mathbf{27}} \equiv \mathbf{27}$ , and  $\overline{\mathbf{64}} \equiv \mathbf{64}$ . It is easy to show from Equations 4 and 5 that

$$\xi(\overline{\mathbf{R}}; \overline{\mathbf{r}}, \overline{\mathbf{r}'}) = \xi(\mathbf{R}; \mathbf{r}, \mathbf{r}'). \quad (6)$$

Then it can be shown (using Equation 6) that

$$\zeta(\mathbf{R}; \mathbf{r}', \mathbf{r}) = \zeta(\mathbf{R}; \mathbf{r}, \mathbf{r}'). \quad (7)$$

The  $\xi$  and  $\zeta$  needed to construct the omitted tables are presented in Tables 2 and 3. We should note that it is not necessary to construct the tables related by Equations 4 and 5 in order to find the phase factors. They are found by considering the highest-isospin states of the representations in the product. Suppose that such a state and the highest-isospin states coupling to it are described as in Section 1. Then from Equation 3 we find simply that

$$\zeta(\mathbf{R}; \mathbf{r}, \mathbf{r}') = (-1)^{I_h - i_h - i'_h}. \quad (8)$$

If in the reversed product  $\mathbf{r}' \otimes \mathbf{r}$  the highest-isospin state in  $\mathbf{r}'$  that couples to  $I_h$  in  $\mathbf{R}$  has quantum numbers  $y_h'^{rev}$  and  $i_h'^{rev}$ , and the highest isospin in  $\mathbf{r}$  that couples to these two has  $y_h^{rev}$  and  $i_h^{rev}$ . Then

$$\xi(\mathbf{R}; \mathbf{r}, \mathbf{r}') = (-1)^{I_h - i_h^{rev} - i'_h^{rev}} \times \text{sign}[F(\mathbf{R}, Y_h, I_h; \mathbf{r}, y_h^{rev}, i_h^{rev}, \mathbf{r}', y_h'^{rev}, i_h'^{rev})], \quad (9)$$

where  $\text{sign}(x) = x/|x|$ .

### 3 Tables

The tables follow. Table 1 is a list of the products of representations whose isoscalar factors are given in this work. Tables 2 and 3 give the phase factors which are described in the

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<sup>2</sup>Our  $\xi$  is the  $\xi_1$  of [1];  $\zeta$  is  $\xi_3$  of [1].

previous section and which can be used to generate other tables from the ones presented. The tables of isoscalar factors appear last. Tables for  $\mathbf{8} \otimes \mathbf{8}$ ,  $\mathbf{10} \otimes \mathbf{8}$ ,  $\mathbf{10} \otimes \mathbf{10}$ ,  $\overline{\mathbf{10}} \otimes \mathbf{10}$ , and  $\mathbf{27} \otimes \mathbf{8}$  appear in [1] and [2]; they are not reproduced here.

In the tables, a square root is assumed to appear over each entry (signs are outside the square roots). Thus,

$\mathbf{r} \otimes \mathbf{r}'$			$\mathbf{R}$	$\pm C$
	$y$	$i$	$Y$	
	$y'$	$i'$	$I$	

(10)

means that the isoscalar factor

$$F(\mathbf{R}, Y, I; \mathbf{r}, y, i, \mathbf{r}', y', i') = \pm\sqrt{C}. \quad (11)$$

### Acknowledgements

We wish to thank J. J. de Swart for his explanation of his phase conventions and for his hospitality.

This work was supported by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U.S. Department of Energy under Contract DE-AC03-76SF00098.

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Table 1: List of tables of isoscalar factors that follow.

Table 4	<b>3</b>	$\otimes$	<b>3</b>	=	<b>6</b>	$\oplus$	<b>3̄</b>
Table 5	<b>3̄</b>	$\otimes$	<b>3</b>	=	<b>8</b>	$\oplus$	<b>1</b>
Table 6	<b>6</b>	$\otimes$	<b>3</b>	=	<b>10</b>	$\oplus$	<b>8</b>
Table 7	<b>6</b>	$\otimes$	<b>3̄</b>	=	<b>15</b>	$\oplus$	<b>3</b>
Table 8	<b>6</b>	$\otimes$	<b>6</b>	=	<b>15'</b>	$\oplus$	<b>15</b> $\oplus$ <b>6̄</b>
Table 9	<b>6̄</b>	$\otimes$	<b>6</b>	=	<b>27</b>	$\oplus$	<b>8</b> $\oplus$ <b>1</b>
Table 10	<b>8</b>	$\otimes$	<b>3</b>	=	<b>15</b>	$\oplus$	<b>6̄</b> $\oplus$ <b>3</b>
Table 11	<b>8</b>	$\otimes$	<b>6</b>	=	<b>24̄</b>	$\oplus$	<b>15̄</b> $\oplus$ <b>6</b> $\oplus$ <b>3̄</b>
Table 12	<b>10</b>	$\otimes$	<b>3</b>	=	<b>15'</b>	$\oplus$	<b>15</b>
Table 13	<b>10</b>	$\otimes$	<b>3̄</b>	=	<b>24̄</b>	$\oplus$	<b>6</b>
Table 14	<b>10</b>	$\otimes$	<b>6</b>	=	<b>21̄</b>	$\oplus$	<b>24̄</b> $\oplus$ <b>15̄</b>
Table 15	<b>10</b>	$\otimes$	<b>6̄</b>	=	<b>42</b>	$\oplus$	<b>15</b> $\oplus$ <b>3</b>
Table 16	<b>15</b>	$\otimes$	<b>3</b>	=	<b>24̄</b>	$\oplus$	<b>15̄</b> $\oplus$ <b>6</b>
Table 17	<b>15</b>	$\otimes$	<b>3̄</b>	=	<b>27</b>	$\oplus$	<b>10</b> $\oplus$ <b>8</b>
Table 18	<b>15</b>	$\otimes$	<b>6</b>	=	<b>35</b>	$\oplus$	<b>27</b> $\oplus$ <b>10̄</b> $\oplus$ <b>10</b> $\oplus$ <b>8</b>
Table 19	<b>15</b>	$\otimes$	<b>6̄</b>	=	<b>42̄</b>	$\oplus$	<b>24̄</b> $\oplus$ <b>15̄</b> $\oplus$ <b>6</b> $\oplus$ <b>3̄</b>
Table 20	<b>15</b>	$\otimes$	<b>8</b>	=	<b>42</b>	$\oplus$	<b>15'</b> $\oplus$ <b>24</b> $\oplus$ <b>15<sub>1</sub></b> $\oplus$ <b>15<sub>2</sub></b> $\oplus$ <b>6̄</b> $\oplus$ <b>3</b>
Table 21	<b>15</b>	$\otimes$	<b>10</b>	=	<b>48</b>	$\oplus$	<b>42</b> $\oplus$ <b>24</b> $\oplus$ <b>15'</b> $\oplus$ <b>15</b> $\oplus$ <b>6̄</b>
Table 22	<b>15'</b>	$\otimes$	<b>3</b>	=	<b>21̄</b>	$\oplus$	<b>24̄</b>
Table 23	<b>15'</b>	$\otimes$	<b>3̄</b>	=	<b>35</b>	$\oplus$	<b>10</b>
Table 24	<b>15'</b>	$\otimes$	<b>6</b>	=	<b>28</b>	$\oplus$	<b>35</b> $\oplus$ <b>27</b>
Table 25	<b>15'</b>	$\otimes$	<b>6̄</b>	=	<b>60̄</b>	$\oplus$	<b>24̄</b> $\oplus$ <b>6</b>
Table 26	<b>15'</b>	$\otimes$	<b>8</b>	=	<b>48</b>	$\oplus$	<b>42</b> $\oplus$ <b>15'</b> $\oplus$ <b>15</b>
Table 27	<b>15'</b>	$\otimes$	<b>10</b>	=	<b>36</b>	$\oplus$	<b>48</b> $\oplus$ <b>42</b> $\oplus$ <b>24</b>
Table 28	<b>15'</b>	$\otimes$	<b>15'</b>	=	<b>45̄</b>	$\oplus$	<b>63̄</b> $\oplus$ <b>60̄</b> $\oplus$ <b>42̄</b> $\oplus$ <b>15'</b>

Table 29	$\overline{21} \otimes 3 = 28 \oplus 35$
Table 30	$\overline{21} \otimes \overline{3} = 48 \oplus 15'$
Table 31	$\overline{21} \otimes 6 = 36 \oplus 48 \oplus 42$
Table 32	$\overline{21} \otimes \overline{6} = 81 \oplus 35 \oplus 10$
Table 33	$\overline{21} \otimes 8 = \overline{63} \oplus \overline{60} \oplus \overline{21} \oplus \overline{24}$
Table 34	$\overline{21} \otimes 10 = \overline{45} \oplus \overline{63} \oplus \overline{60} \oplus \overline{42}$
Table 35	$\overline{24} \otimes 3 = 35 \oplus 27 \oplus 10$
Table 36	$\overline{24} \otimes \overline{3} = 42 \oplus 15' \oplus 15$
Table 37	$\overline{24} \otimes 6 = 48 \oplus 42 \oplus 24 \oplus 15' \oplus 15$
Table 38	$\overline{24} \otimes 8 = \overline{60} \oplus \overline{42} \oplus \overline{21} \oplus \overline{24}_1 \oplus \overline{24}_2 \oplus \overline{15} \oplus 6$
Table 39	$\overline{27} \otimes 3 = 42 \oplus 24 \oplus 15$
Table 40	$\overline{27} \otimes 6 = \overline{60} \oplus \overline{42} \oplus \overline{24} \oplus \overline{15'} \oplus \overline{15} \oplus 6$
Table 41	$\overline{28} \otimes 3 = 36 \oplus 48$
Table 42	$\overline{28} \otimes \overline{3} = \overline{63} \oplus \overline{21}$
Table 43	$\overline{28} \otimes 6 = \overline{45} \oplus \overline{63} \oplus \overline{60}$
Table 44	$\overline{35} \otimes 3 = 48 \oplus 42 \oplus 15'$
Table 45	$\overline{35} \otimes \overline{3} = \overline{60} \oplus \overline{21} \oplus \overline{24}$
Table 46	$\overline{35} \otimes 6 = \overline{63} \oplus \overline{60} \oplus \overline{42} \oplus \overline{21} \oplus \overline{24}$
Table 47	$\overline{36} \otimes 3 = \overline{45} \oplus \overline{63}$
Table 48	$\overline{36} \otimes \overline{3} = 80 \oplus 28$

Table 2: Phase factors  $\xi$ . Here (+) denotes +1 and (-) denotes -1.

$\xi$	R								
r r'	1	8	10	$\overline{10}$	27	35	28	81	80
$\overline{3} \ 3$	-	+							
$6 \ 3$		-	+						
$\overline{6} \ 6$	+	-				+			
$15 \ \overline{3}$		-	-		+				
$15 \ 6$		+	-	+	-	+			
$15' \ \overline{3}$			-			+			
$15' \ 6$					+	-	+		
$\overline{21} \ 3$						-	+		
$\overline{21} \ \overline{6}$			+			-		+	
$\overline{24} \ 3$			-		-	+			
$36 \ \overline{3}$							-		+

$\xi$	R									
r r'	3	$\overline{6}$	$15_1$	$15_2$	$15'$	24	42	48	36	
$6 \ \overline{3}$	-		+							
$6 \ 6$		+	-		+					
$8 \ 3$	-	-	+							
$10 \ 3$			-		+					
$10 \ \overline{6}$	+	-					+			
$15 \ 8$	+	+	+	-	-	-	-	+		
$15 \ 10$	-	+			-	+	-	+		
$15' \ 8$		+		-			-	+		
$15' \ 10$						-	+	-	+	
$\overline{21} \ \overline{3}$						-			+	
$\overline{21} \ 6$							+	-	+	
$\overline{24} \ \overline{3}$			-			-		+		
$\overline{24} \ 6$			+		-	+	-	+		
$27 \ 3$			-			-	+			
$28 \ 3$								-	+	
$35 \ 3$						-	-	+		

$\xi$	R											
r	r'	3	6	15	15'	24 <sub>1</sub>	24 <sub>2</sub>	21	42	60	63	45
3	3	-	+									
8	6	+	-	-			+					
10	3		-				+					
10	6			+		-			+			
15	3		-	-		+						
15	6	+	+	-		-				+		
15'	3				+			-		+		
15'	6	+			-					+		
15'	15'			+				-	+	-	-	+
21	8				+			-		-	+	
21	10								-	+	-	+
24	8	+	+		+	-	-	-	-	+		
27	6	+	+	+	-				-	+		
28	3							-			+	
28	6									+	-	+
35	3				-			-		+		
35	6				+			-	+	-	+	
36	3									-	+	

Table 3: Phase factors  $\zeta$ . Here (+) denotes +1 and (-) denotes -1.

$\zeta$		R								
r	r'	1	8	10	$\overline{10}$	27	35	28	81	80
$\overline{3}$	3	-	+							
6	3		+	+						
$\overline{6}$	6	+	-			+				
15	$\overline{3}$		-	+		+				
15	6		-	-	+	+	+			
$15'$	$\overline{3}$			-			+			
$15'$	6					+	+	+		
$\overline{21}$	3						+	+		
$\overline{21}$	$\overline{6}$			+			-		+	
$\overline{24}$	3		-		+	+				
36	$\overline{3}$						-		+	

$\zeta$		R								
r	r'	3	$\overline{6}$	$15_1$	$15_2$	$15'$	24	42	48	36
6	$\overline{3}$	-		+						
6	6		+	+			+			
8	3	-	+	+						
10	3			+		+				
10	$\overline{6}$	+	-					+		
15	8	+	-	+	-	+	+	+	+	
15	10	-	-			-	+	+	+	
$15'$	8	-			-		+	+		
$15'$	10					+	+	+	+	
$\overline{21}$	3					-			+	
$\overline{21}$	6						+	+	+	
$\overline{24}$	3		-		+		+			
$\overline{24}$	6		-		-	+	+	+		
28	3							+	+	
27	3		-			+	+			
35	3				-		+	+		

$\zeta$	R											
r	r'	3	6	$\bar{15}_1$	$\bar{15}'$	$\bar{24}_1$	$\bar{24}_2$	$\bar{21}$	$\bar{42}$	$\bar{60}$	$\bar{63}$	$\bar{45}$
3	3	+	+									
8	6	-	-	+			+					
10	$\bar{3}$		-				+					
10	6			+		+		+				
15	3		-	+		+						
15	$\bar{6}$	+	-	-		+			+			
$15'$	3		-	+		+						
$15'$	$\bar{6}$	+	-	-		+			+			
$15'$	$15'$				+			+	+	+	+	
$\bar{21}$	8					-		-	+	+		
$\bar{21}$	10							+	+	+	+	
$\bar{24}$	8	+	-		+	-	+	+	+			
27	6	+	-	+	-			+	+			
28	$\bar{3}$						-			+		
28	6								+	+	+	
35	$\bar{3}$				-		+		+			
35	6				+		-	+	+	+		
36	3								+	+		

Table 4: Isoscalar factors for  $\mathbf{3} \otimes \mathbf{3}$ . Notation for this and following tables is explained in the text. In these tables a square root is assumed over each entry.

$\mathbf{3} \otimes \mathbf{3}$	$\bar{\mathbf{3}} \quad \mathbf{6} \quad \bar{\mathbf{3}} \quad \mathbf{6} \quad \mathbf{6}$			
$\frac{2}{3}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$
$0$	$1$	$\frac{1}{2}$	$\frac{1}{2}$	$0$
$\frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	$-1$	$1$		
$\frac{1}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 0$			$\frac{1}{2} \quad \frac{1}{2}$	
$-\frac{2}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$			$-\frac{1}{2} \quad \frac{1}{2}$	
$-\frac{2}{3} \quad 0 \quad -\frac{2}{3} \quad 0$				$1$

Table 5: Isoscalar factors for  $\bar{\mathbf{3}} \otimes \mathbf{3}$ .

$\bar{\mathbf{3}} \otimes \mathbf{3}$	$8 \quad 1 \quad 8 \quad 8 \quad 8$
$1$	$0 \quad 0 \quad 0 \quad 0 \quad -1$
$\frac{1}{2}$	$0 \quad 0 \quad 1 \quad \frac{1}{2}$
$\frac{2}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$	$1$
$\frac{2}{3} \quad 0 \quad -\frac{2}{3} \quad 0$	$\frac{1}{3} \quad \frac{2}{3}$
$-\frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	$\frac{2}{3} \quad -\frac{1}{3}$
$-\frac{1}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 0$	$1$

Table 6: Isoscalar factors for  $\mathbf{6} \otimes \mathbf{3}$ .

$\mathbf{6} \otimes \mathbf{3}$	$8 \quad 10 \quad 8 \quad 8 \quad 10 \quad 8 \quad 10 \quad 10$
$1$	$1 \quad 0 \quad 0 \quad 0 \quad 0 \quad -1 \quad -1 \quad -2$
$\frac{1}{2}$	$\frac{3}{2} \quad 0 \quad 1 \quad 1 \quad \frac{1}{2} \quad \frac{1}{2} \quad 0$
$\frac{2}{3} \quad 1 \quad \frac{1}{3} \quad \frac{1}{2}$	$-1 \quad 1$
$-\frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	$-1 \quad -\frac{1}{3} \quad \frac{2}{3}$
$\frac{2}{3} \quad 1 \quad -\frac{2}{3} \quad 0$	$\frac{2}{3} \quad \frac{1}{3}$
$-\frac{1}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 0$	$\frac{1}{3} \quad \frac{2}{3}$
$-\frac{4}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$	$-\frac{2}{3} \quad \frac{1}{3}$
$-\frac{4}{3} \quad 0 \quad -\frac{2}{3} \quad 0$	$1$

Table 7: Isoscalar factors for  $\mathbf{6} \otimes \overline{\mathbf{3}}$ .

$\mathbf{6} \otimes \overline{\mathbf{3}}$	15	3	15	15	3	15	15	15
	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$
	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	0	0	1	$\frac{1}{2}$
$\frac{2}{3}$	1	$\frac{2}{3}$	0	1				
$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	0		$-\frac{1}{4}$	$\frac{3}{4}$		
$\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$		$\frac{3}{4}$	$\frac{1}{4}$	1	
$-\frac{4}{3}$	0	$\frac{2}{3}$	0			$-\frac{1}{2}$	$\frac{1}{2}$	
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$			$\frac{1}{2}$	$\frac{1}{2}$	1
$-\frac{4}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$					1

 Table 8: Isoscalar factors for  $\mathbf{6} \otimes \mathbf{6}$ .

$\mathbf{6} \otimes \mathbf{6}$	$\overline{\mathbf{6}}$	15	$15'$	$\overline{\mathbf{6}}$	15	15	$15'$	15	$\overline{\mathbf{6}}$	15	$15'$	15	$15'$	$15'$
	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$
	0	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	0
$\frac{2}{3}$	1	$\frac{2}{3}$	1	1	-1	1								
$\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$				$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$				
$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1				$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$				
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$								-1	$-\frac{1}{3}$	0	$\frac{2}{3}$
$\frac{2}{3}$	1	$-\frac{4}{3}$	0									$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{6}$
$-\frac{4}{3}$	0	$\frac{2}{3}$	1									$\frac{1}{3}$	$-\frac{1}{2}$	$\frac{1}{6}$
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0									$\frac{1}{2}$	$\frac{1}{2}$	
$-\frac{4}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$									$-\frac{1}{2}$	$\frac{1}{2}$	
$-\frac{4}{3}$	0	$-\frac{4}{3}$	0											1

Table 9: Isoscalar factors for  $\bar{\mathbf{6}} \otimes \mathbf{6}$ .

$\bar{\mathbf{6}} \otimes \mathbf{6}$		$27 \ 8 \ 27 \ 27 \ 1 \ 8 \ 27 \ 8 \ 27 \ 27 \ 27 \ 8 \ 27 \ 27 \ 27$
		2 1 1 1 0 0 0 0 0 0 -1 -1 -1 -2
		1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{3}{2}$ 0 0 0 1 1 2 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{3}{2}$ 1
$\frac{4}{3} \ 0 \ \frac{2}{3} \ 1$	1	
$\frac{4}{3} \ 0 \ -\frac{1}{3} \ \frac{1}{2}$	$\frac{2}{5} \ \frac{3}{5}$	
$\frac{1}{3} \ \frac{1}{2} \ \frac{2}{3} \ 1$	$\frac{3}{5} \ -\frac{2}{5}$	1
$\frac{4}{3} \ 0 \ -\frac{4}{3} \ 0$		$\frac{1}{6} \ \frac{8}{15} \ \frac{3}{10}$
$\frac{1}{3} \ \frac{1}{2} \ -\frac{1}{3} \ \frac{1}{2}$		$\frac{1}{3} \ \frac{1}{15} \ -\frac{3}{5}$
$-\frac{2}{3} \ 1 \ \frac{2}{3} \ 1$		$\frac{1}{2} \ -\frac{2}{5} \ \frac{1}{10} \ \frac{4}{5} \ -\frac{1}{5}$
$\frac{1}{3} \ \frac{1}{2} \ -\frac{4}{3} \ 0$		
$-\frac{2}{3} \ 1 \ -\frac{1}{3} \ \frac{1}{2}$		$\frac{2}{5} \ \frac{3}{5}$
$-\frac{2}{3} \ 1 \ -\frac{4}{3} \ 0$		$\frac{3}{5} \ -\frac{2}{5}$
		1
		1

 Table 10: Isoscalar factors for  $\mathbf{8} \otimes \mathbf{3}$ .

$\mathbf{8} \otimes \mathbf{3}$		$\bar{\mathbf{6}} \ 15 \ 3 \ \bar{\mathbf{6}} \ 15 \ 15 \ 15 \ 3 \ 15 \ \bar{\mathbf{6}} \ 15 \ 15$
		$\frac{4}{3} \ \frac{4}{3} \ \frac{1}{3} \ \frac{1}{3} \ \frac{1}{3} \ \frac{1}{3} \ -\frac{2}{3} \ -\frac{2}{3} \ -\frac{2}{3} \ -\frac{5}{3}$
		0 1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{3}{2}$ 0 0 1 1 $\frac{1}{2}$
$1 \ \frac{1}{2} \ \frac{1}{3} \ \frac{1}{2}$	-1 1	
$1 \ \frac{1}{2} \ -\frac{2}{3} \ 0$		$\frac{3}{8} \ \frac{1}{4} \ \frac{3}{8}$
$0 \ 0 \ \frac{1}{3} \ \frac{1}{2}$		$-\frac{1}{16} \ -\frac{3}{8} \ \frac{9}{16}$
$0 \ 1 \ \frac{1}{3} \ \frac{1}{2}$		$\frac{9}{16} \ -\frac{3}{8} \ -\frac{1}{16}$
$0 \ 0 \ -\frac{2}{3} \ 0$		$\frac{1}{4} \ \frac{3}{4}$
$-1 \ \frac{1}{2} \ \frac{1}{3} \ \frac{1}{2}$		$\frac{3}{4} \ -\frac{1}{4}$
$0 \ 1 \ -\frac{2}{3} \ 0$		$-\frac{1}{2} \ \frac{1}{2}$
$-1 \ \frac{1}{2} \ -\frac{2}{3} \ 0$		$\frac{1}{2} \ \frac{1}{2}$
		1

Table 11: Isoscalar factors for  $\mathbf{8} \otimes \mathbf{6}$ .

$\mathbf{8} \otimes \mathbf{6}$			$\overline{\mathbf{15}}$	$\mathbf{24}$	$\overline{\mathbf{3}}$	$\overline{\mathbf{15}}$	$\mathbf{6}$	$\overline{\mathbf{15}}$	$\mathbf{24}$	$\overline{\mathbf{24}}$
			$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
			$\frac{1}{2}$	$\frac{3}{2}$	0	0	1	1	1	2
1	$\frac{1}{2}$	$\frac{2}{3}$	1	-1	1					
1	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$			$-\frac{1}{4}$	$-\frac{3}{4}$	$\frac{3}{10}$	$\frac{1}{6}$	$\frac{8}{15}$
0	1	$\frac{2}{3}$	1			$-\frac{3}{4}$	$\frac{1}{4}$	$\frac{3}{5}$	$-\frac{1}{3}$	$-\frac{1}{15}$
0	0	$\frac{2}{3}$	1					$-\frac{1}{10}$	$-\frac{1}{2}$	$\frac{2}{5}$

$\mathbf{8} \otimes \mathbf{6}$			$\overline{\mathbf{3}}$	$\mathbf{6}$	$\overline{\mathbf{15}}$	$\mathbf{24}$	$\overline{\mathbf{15}}$	$\mathbf{24}$	$\overline{\mathbf{24}}$	$\mathbf{6}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{15}}$	$\mathbf{24}$	$\overline{\mathbf{24}}$
			$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{7}{3}$
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
1	$\frac{1}{2}$	$-\frac{4}{3}$	0	$\frac{1}{4}$	$\frac{3}{10}$	$\frac{1}{4}$	$\frac{1}{5}$							
0	0	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{3}{16}$	$\frac{1}{40}$	$-\frac{3}{16}$	$\frac{3}{5}$							
0	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{3}{16}$	$\frac{9}{40}$	$-\frac{25}{48}$	$-\frac{1}{15}$	$\frac{1}{3}$	$\frac{2}{3}$					
-1	$\frac{1}{2}$	$\frac{2}{3}$	1	$-\frac{3}{8}$	$\frac{9}{20}$	$\frac{1}{24}$	$-\frac{2}{15}$	$-\frac{2}{3}$	$\frac{1}{3}$					
0	0	$-\frac{4}{3}$	0					$\frac{2}{5}$	$\frac{3}{5}$					
-1	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$					$\frac{3}{5}$	$-\frac{2}{5}$	$-\frac{1}{3}$	$\frac{2}{3}$			
0	1	$-\frac{4}{3}$	0					$\frac{2}{3}$	$\frac{1}{3}$					
-1	$\frac{1}{2}$	$-\frac{4}{3}$	0											1

 Table 12: Isoscalar factors for  $\mathbf{10} \otimes \mathbf{3}$ .

$\mathbf{10} \otimes \mathbf{3}$			$\mathbf{15}$	$\mathbf{15}'$	$\mathbf{15}$	$\mathbf{15}$	$\mathbf{15}'$	$\mathbf{15}$	$\mathbf{15}$	$\mathbf{15}'$	$\mathbf{15}$	$\mathbf{15}'$	$\mathbf{15}'$	
			$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	
			1	2	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	$\frac{1}{2}$	$\frac{1}{2}$	
1	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$	-1	1									
0	1	$\frac{1}{3}$	$\frac{1}{2}$			$-1$	$-\frac{1}{4}$	$\frac{3}{4}$						
1	$\frac{3}{2}$	$-\frac{2}{3}$	0				$\frac{3}{4}$	$\frac{1}{4}$						
-1	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$					$-1$	$-\frac{1}{2}$	$\frac{1}{2}$				
0	1	$-\frac{2}{3}$	0					$\frac{1}{2}$	$\frac{1}{2}$					
-1	$\frac{1}{2}$	$-\frac{2}{3}$	0							$\frac{1}{4}$	$\frac{3}{4}$			
-2	0	$\frac{1}{3}$	$\frac{1}{2}$							$-\frac{3}{4}$	$\frac{1}{4}$			
-2	0	$-\frac{2}{3}$	0											1

Table 13: Isoscalar factors for  $\mathbf{10} \otimes \overline{\mathbf{3}}$ .

$\mathbf{10} \otimes \overline{\mathbf{3}}$	$\overline{\mathbf{24}}$	$\mathbf{6}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{24}}$	$\mathbf{6}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{24}}$	$\mathbf{6}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{24}}$
	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{7}{3}$
	$\frac{3}{2}$	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	0	0	1	$\frac{1}{2}$
1 $\frac{3}{2}$ $\frac{2}{3}$ 0	1										
0 1 $\frac{2}{3}$ 0		$-\frac{1}{5}$	$\frac{4}{5}$								
1 $\frac{3}{2}$ $-\frac{1}{3}$ $\frac{1}{2}$		$\frac{4}{5}$	$\frac{1}{5}$	1							
-1 $\frac{1}{2}$ $\frac{2}{3}$ 0					$-\frac{2}{5}$	$\frac{3}{5}$					
0 1 $-\frac{1}{3}$ $\frac{1}{2}$					$\frac{3}{5}$	$\frac{2}{5}$	1				
-2 0 $\frac{2}{3}$ 0								$-\frac{3}{5}$	$\frac{2}{5}$		
-1 $\frac{1}{2}$ $-\frac{1}{3}$ $\frac{1}{2}$								$\frac{2}{5}$	$\frac{3}{5}$	1	
-2 0 $-\frac{1}{3}$ $\frac{1}{2}$											1

 Table 14: Isoscalar factors for  $\mathbf{10} \otimes \mathbf{6}$ .

$\mathbf{10} \otimes \mathbf{6}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$
	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	0	1	1	2	2
1 $\frac{3}{2}$ $\frac{2}{3}$ 1	1	-1	1					
0 1 $\frac{2}{3}$ 1				1	$\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{2}{5}$	$\frac{3}{5}$
1 $\frac{3}{2}$ $-\frac{1}{3}$ $\frac{1}{2}$					$-\frac{2}{3}$	$-\frac{1}{3}$	$\frac{3}{5}$	$\frac{2}{5}$

$\mathbf{10} \otimes \mathbf{6}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{21}}$
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	0
0 1 $-\frac{1}{3}$ $\frac{1}{2}$	$-\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{15}$	$\frac{3}{5}$							
-1 $\frac{1}{2}$ $\frac{2}{3}$ 1	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{1}{6}$	$-\frac{8}{15}$	$\frac{3}{10}$							
1 $\frac{3}{2}$ $-\frac{4}{3}$ 0			$\frac{1}{2}$	$\frac{2}{5}$	$\frac{1}{10}$							
-1 $\frac{1}{2}$ $-\frac{1}{3}$ $\frac{1}{2}$						-1	$-\frac{1}{3}$	$-\frac{1}{15}$	$\frac{3}{5}$			
0 1 $-\frac{4}{3}$ 0							$\frac{1}{6}$	$\frac{8}{15}$	$\frac{3}{10}$			
-2 0 $\frac{2}{3}$ 1							$\frac{1}{2}$	$-\frac{2}{5}$	$\frac{1}{10}$			
-1 $\frac{1}{2}$ $-\frac{4}{3}$ 0										$\frac{2}{5}$	$\frac{3}{5}$	
-2 0 $-\frac{1}{3}$ $\frac{1}{2}$										$-\frac{3}{5}$	$\frac{2}{5}$	
-2 0 $-\frac{4}{3}$ 0												1

Table 15: Isoscalar factors for  $\mathbf{10} \otimes \overline{\mathbf{6}}$ .

$\mathbf{10} \otimes \overline{\mathbf{6}}$ .	42	15	42	42	3	15	42	15	42	42
	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
	$\frac{3}{2}$	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$
1 $\frac{3}{2}$ $\frac{4}{3}$ 0	1									
0 1 $\frac{4}{3}$ 0		$-\frac{1}{3}$	$\frac{2}{3}$							
1 $\frac{3}{2}$ $\frac{1}{3}$ $\frac{1}{2}$		$\frac{2}{3}$	$\frac{1}{3}$	1						
-1 $\frac{1}{2}$ $\frac{4}{3}$ 0					$\frac{1}{10}$	$-\frac{1}{2}$	$\frac{2}{5}$			
0 1 $\frac{1}{3}$ $\frac{1}{2}$					$-\frac{3}{10}$	$\frac{1}{6}$	$\frac{8}{15}$	$-\frac{1}{6}$	$\frac{5}{6}$	
1 $\frac{3}{2}$ $-\frac{2}{3}$ 1					$\frac{3}{5}$	$\frac{1}{3}$	$\frac{1}{15}$	$\frac{5}{6}$	$\frac{1}{6}$	1

  

$\mathbf{10} \otimes \overline{\mathbf{6}}$	3	15	42	15	42	42	15	42	42	42
	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$
	0	0	0	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	1
-2 0 $\frac{4}{3}$ 0	$\frac{3}{10}$	$-\frac{1}{2}$	$\frac{1}{5}$							
-1 $\frac{1}{2}$ $\frac{1}{3}$ $\frac{1}{2}$	$-\frac{2}{5}$	0	$\frac{3}{5}$	$-\frac{1}{3}$	$\frac{2}{3}$					
0 1 $-\frac{2}{3}$ 1	$\frac{3}{10}$	$\frac{1}{2}$	$\frac{1}{5}$	$\frac{2}{3}$	$\frac{1}{3}$	1				
-2 0 $\frac{1}{3}$ $\frac{1}{2}$							$-\frac{1}{2}$	$\frac{1}{2}$		
-1 $\frac{1}{2}$ $-\frac{2}{3}$ 1							$\frac{1}{2}$	$\frac{1}{2}$	1	
-2 0 $-\frac{2}{3}$ 1										1

Table 16: Isoscalar factors for  $\mathbf{15} \otimes \mathbf{3}$ .

$\mathbf{15} \otimes \mathbf{3}$	15	24	15	6	15	24	24	6	15	24	15	24	6	24	15	24	24
	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{7}{3}$
	$\frac{1}{2}$	$\frac{3}{2}$	0	1	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
$\frac{4}{3}$	1	$\frac{1}{3}$	$\frac{1}{2}$	-1	1												
$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$			-1	$-\frac{1}{15}$	$-\frac{2}{9}$	$\frac{32}{45}$								
$\frac{4}{3}$	1	$-\frac{2}{3}$	0				$\frac{2}{5}$	$\frac{1}{3}$	$\frac{4}{15}$								
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$				$\frac{8}{15}$	$-\frac{4}{9}$	$-\frac{1}{45}$	1							
$\frac{1}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	0								$\frac{3}{10}$	$\frac{1}{6}$	$\frac{8}{15}$				
$-\frac{2}{3}$	0	$\frac{1}{3}$	$\frac{1}{2}$								$-\frac{1}{10}$	$-\frac{1}{2}$	$\frac{2}{5}$				
$-\frac{2}{3}$	1	$\frac{1}{3}$	$\frac{1}{2}$								$\frac{3}{5}$	$-\frac{1}{3}$	$-\frac{1}{15}$	$-\frac{1}{3}$	$\frac{2}{3}$		
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{2}{3}$	0									$\frac{2}{3}$	$\frac{1}{3}$				
$-\frac{2}{3}$	0	$-\frac{2}{3}$	0									$\frac{1}{5}$	$\frac{4}{5}$				
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$									$\frac{4}{5}$	$-\frac{1}{5}$	$-\frac{2}{3}$	$\frac{1}{3}$		
$-\frac{2}{3}$	1	$-\frac{2}{3}$	0										$\frac{1}{3}$	$\frac{2}{3}$			
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	0														1

 Table 17: Isoscalar factors for  $\mathbf{15} \otimes \overline{\mathbf{3}}$ .

$\mathbf{15} \otimes \overline{\mathbf{3}}$	27	8	27	10	27	8	27	8	10	27	27	8	10	27	27	10	27
	2	1	1	1	1	0	0	0	0	0	0	-1	-1	-1	-1	-2	-2
	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	0	1
$\frac{4}{3}$	1	$\frac{2}{3}$	0	1		1											
$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	0			$-\frac{1}{5}$	$\frac{4}{5}$										
$\frac{4}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{4}{5}$	$\frac{1}{5}$	$-\frac{1}{2}$	$\frac{1}{2}$										
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{2}{3}$	0			$\frac{1}{2}$	$\frac{1}{2}$										
$-\frac{2}{3}$	0	$\frac{2}{3}$	0					$-\frac{2}{5}$	$\frac{3}{5}$								
$\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{3}{5}$	$\frac{2}{5}$	$\frac{1}{5}$	$\frac{2}{5}$					$\frac{1}{45}$	$-\frac{4}{9}$	$\frac{8}{15}$			
$-\frac{2}{3}$	1	$\frac{2}{3}$	0					$-\frac{4}{15}$	$\frac{1}{3}$	$\frac{2}{5}$							
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{32}{45}$	$\frac{2}{9}$	$\frac{1}{15}$	1										
$-\frac{2}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$								$\frac{1}{15}$	$-\frac{1}{3}$	$\frac{3}{5}$				
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	0								$-\frac{8}{15}$	$\frac{1}{6}$	$\frac{3}{10}$				
$-\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$								$\frac{2}{5}$	$\frac{1}{2}$	$\frac{1}{10}$	1			
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$												1	1	

Table 18: Isoscalar factors for  $\mathbf{15} \otimes \mathbf{6}$ .

$\mathbf{15} \otimes \mathbf{6}$		$\overline{\mathbf{10}}$	$\mathbf{27}$	$\mathbf{35}$	$\mathbf{8}$	$\overline{\mathbf{10}}$	$\mathbf{27}$	$\mathbf{10}$	$\mathbf{27}$	$\mathbf{35}$	$\mathbf{35}$	
		2	2	2	1	1	1	1	1	1	1	
		0	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	
$\frac{4}{3}$	1	$\frac{2}{3}$	1	1	-1	1						
$\frac{4}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$				$-\frac{4}{15}$	$-\frac{1}{3}$	$-\frac{2}{5}$	$\frac{1}{3}$	$\frac{1}{4}$	$\frac{5}{12}$
$\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1				$\frac{1}{45}$	$\frac{4}{9}$	$-\frac{8}{15}$	$-\frac{1}{9}$	$-\frac{1}{3}$	$\frac{5}{9}$
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{2}{3}$	1				$-\frac{32}{45}$	$\frac{2}{9}$	$\frac{1}{15}$	$\frac{5}{9}$	$-\frac{5}{12}$	$-\frac{1}{36}$
												1

$\mathbf{15} \otimes \mathbf{6}$		$\mathbf{8}$	$\mathbf{27}$	$\mathbf{8}$	$\mathbf{10}$	$\overline{\mathbf{10}}$	$\mathbf{27}$	$\mathbf{35}$	$\mathbf{27}$	$\mathbf{35}$		
		0	0	0	0	0	0	0	0	0		
		0	0	1	1	1	1	1	1	2		
$\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{5}$	$-\frac{4}{5}$	$-\frac{5}{27}$	$\frac{2}{27}$	$-\frac{4}{27}$	0	$\frac{16}{27}$		
$-\frac{2}{3}$	1	$\frac{2}{3}$	1	$-\frac{4}{5}$	$\frac{1}{5}$	$-\frac{8}{45}$	$\frac{4}{9}$	$\frac{2}{9}$	$-\frac{1}{10}$	$-\frac{1}{18}$	$-\frac{1}{2}$	$\frac{1}{2}$
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$			$\frac{32}{135}$	$\frac{4}{27}$	$-\frac{8}{27}$	$-\frac{3}{10}$	$-\frac{1}{54}$	$\frac{1}{2}$	$\frac{1}{2}$
$\frac{4}{3}$	1	$-\frac{4}{3}$	0			$\frac{16}{45}$	$\frac{2}{9}$	$\frac{1}{9}$	$\frac{1}{5}$	$\frac{1}{9}$		
$-\frac{2}{3}$	0	$\frac{2}{3}$	1			$\frac{2}{45}$	$-\frac{1}{9}$	$\frac{2}{9}$	$-\frac{2}{5}$	$\frac{2}{9}$		

$\mathbf{15} \otimes \mathbf{6}$		$\mathbf{8}$	$\mathbf{10}$	$\mathbf{27}$	$\mathbf{35}$	$\overline{\mathbf{10}}$	$\mathbf{27}$	$\mathbf{35}$	$\mathbf{10}$	$\mathbf{35}$	$\mathbf{27}$	$\mathbf{35}$	$\mathbf{35}$
		-1	-1	-1	-1	-1	-1	-1	-2	-2	-2	-2	-3
		$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
$\frac{1}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0	$\frac{2}{15}$	$\frac{1}{3}$	$\frac{1}{5}$	$\frac{1}{3}$						
$-\frac{2}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{5}$	0	$-\frac{3}{10}$	$\frac{1}{2}$						
$-\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{15}$	$\frac{1}{3}$	$-\frac{9}{20}$	$-\frac{1}{12}$	$-\frac{1}{3}$	0	$\frac{2}{3}$			
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1	$-\frac{8}{15}$	$\frac{1}{3}$	$\frac{1}{20}$	$-\frac{1}{12}$	$\frac{1}{3}$	$-\frac{1}{2}$	$\frac{1}{6}$			
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{4}{3}$	0					$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{6}$			
$-\frac{2}{3}$	0	$-\frac{4}{3}$	0						$\frac{1}{3}$	$\frac{2}{3}$			
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$					$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{2}$	$\frac{1}{2}$		
$-\frac{2}{3}$	1	$-\frac{4}{3}$	0							$\frac{1}{2}$	$\frac{1}{2}$		
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0										1

Table 19: Isoscalar factors for  $\mathbf{15} \otimes \overline{\mathbf{6}}$ .

$\mathbf{15} \otimes \overline{\mathbf{6}}$	$\overline{\mathbf{42}} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{3}} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{42}} \quad \mathbf{6} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}}$		
$\frac{8}{3} \quad \frac{5}{3} \quad \frac{5}{3} \quad \frac{5}{3} \quad \frac{5}{3} \quad \frac{2}{3} \quad \frac{2}{3}$			
$1 \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad 0 \quad 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \quad 2 \quad 2$			
$\frac{4}{3} \quad 1 \quad \frac{4}{3} \quad 0$	1		
$\frac{1}{3} \quad \frac{1}{2} \quad \frac{4}{3} \quad 0$	$-\frac{1}{3} \quad \frac{2}{3}$		
$\frac{4}{3} \quad 1 \quad \frac{1}{3} \quad \frac{1}{2}$	$\frac{2}{3} \quad \frac{1}{3}$	$-\frac{1}{3} \quad \frac{2}{3}$	
$\frac{1}{3} \quad \frac{3}{2} \quad \frac{4}{3} \quad 0$	$\frac{2}{3} \quad \frac{1}{3}$		
$-\frac{2}{3} \quad 0 \quad \frac{4}{3} \quad 0$	$\frac{1}{10} \quad -\frac{1}{2} \quad \frac{2}{5}$		
$\frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	$-\frac{3}{10} \quad \frac{1}{6} \quad \frac{8}{15}$	$\frac{2}{15} \quad -\frac{1}{27} \quad -\frac{32}{135} \quad \frac{16}{27}$	
$\frac{4}{3} \quad 1 \quad -\frac{2}{3} \quad 1$	$\frac{3}{5} \quad \frac{1}{3} \quad \frac{1}{15}$	$-\frac{2}{5} \quad \frac{4}{9} \quad -\frac{2}{45} \quad \frac{1}{9}$	$-\frac{2}{3} \quad \frac{1}{3}$
$\frac{1}{3} \quad \frac{3}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	$\frac{4}{15} \quad \frac{8}{27} \quad \frac{49}{135} \quad \frac{2}{27}$	$\frac{1}{3} \quad \frac{2}{3}$	
$-\frac{2}{3} \quad 1 \quad \frac{4}{3} \quad 0$	$-\frac{1}{5} \quad -\frac{2}{9} \quad \frac{16}{45} \quad \frac{2}{9}$		

$\mathbf{15} \otimes \overline{\mathbf{6}}$	$\overline{\mathbf{3}} \quad \mathbf{6} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{42}} \quad \mathbf{6} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{15}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{42}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{42}}$		
$-\frac{1}{3} \quad -\frac{1}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{7}{3} \quad -\frac{7}{3}$			
$\frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad \frac{5}{2} \quad 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 2 \quad \frac{1}{2} \quad \frac{3}{2}$			
$-\frac{5}{3} \quad \frac{1}{2} \quad \frac{4}{3} \quad 0$	$\frac{1}{5} \quad -\frac{1}{5} \quad -\frac{1}{3} \quad \frac{2}{15} \quad \frac{2}{15}$		
$-\frac{2}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$	$-\frac{1}{20} \quad \frac{1}{5} \quad -\frac{1}{12} \quad -\frac{2}{15} \quad \frac{8}{15}$		
$-\frac{2}{3} \quad 1 \quad \frac{1}{3} \quad \frac{1}{2}$	$-\frac{3}{10} \quad 0 \quad \frac{1}{18} \quad \frac{5}{9} \quad \frac{4}{45}$	$-\frac{2}{9} \quad \frac{2}{9} \quad \frac{5}{9}$	
$\frac{1}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 1$	$\frac{1}{20} \quad -\frac{1}{5} \quad \frac{49}{108} \quad -\frac{8}{135} \quad \frac{32}{135}$	$\frac{1}{27} \quad -\frac{16}{27} \quad \frac{10}{27}$	
$\frac{1}{3} \quad \frac{3}{2} \quad -\frac{2}{3} \quad 1$	$\frac{2}{5} \quad \frac{2}{5} \quad \frac{2}{27} \quad \frac{16}{135} \quad \frac{1}{135}$	$\frac{20}{27} \quad \frac{5}{27} \quad \frac{2}{27}$	1
$\frac{5}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$		$-\frac{2}{5} \quad \frac{3}{5} \quad -\frac{4}{9} \quad \frac{1}{9} \quad \frac{4}{9}$	
$\frac{2}{3} \quad 1 \quad -\frac{2}{3} \quad 1$		$\frac{3}{5} \quad \frac{2}{5} \quad \frac{4}{9} \quad \frac{4}{9} \quad \frac{1}{9}$	1
$\frac{2}{3} \quad 0 \quad -\frac{2}{3} \quad 1$		$\frac{1}{9} \quad -\frac{4}{9} \quad \frac{4}{9}$	
$-\frac{5}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 1$			1
			1

Table 20: Isoscalar factors for  $\mathbf{15} \otimes \mathbf{8}$ .

		<b>24</b>	<b>42</b>	<b>6</b>	<b>24</b>	<b>15<sub>1</sub></b>	<b>15<sub>2</sub></b>	<b>24</b>	<b>42</b>	<b>15'</b>	<b>42</b>
<b>15 <math>\otimes</math> 8</b>	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$
	$\frac{1}{2}$	$\frac{3}{2}$	0	0	1	1	1	1	2	2	2
$\frac{4}{3}$	1	1	$\frac{1}{2}$	-1	1						
$\frac{1}{3}$	$\frac{1}{2}$	1	$\frac{1}{2}$			$\frac{1}{5}$	$-\frac{4}{5}$	$-\frac{1}{61}$	$-\frac{400}{1647}$	$-\frac{4}{27}$	$\frac{16}{27}$
$\frac{4}{3}$	1	0	1			$-\frac{4}{5}$	$-\frac{1}{5}$	$\frac{24}{61}$	$\frac{361}{1098}$	$-\frac{2}{9}$	$\frac{1}{18}$
$\frac{1}{3}$	$\frac{3}{2}$	1	$\frac{1}{2}$					$-\frac{32}{61}$	$\frac{529}{3294}$	$-\frac{8}{27}$	$-\frac{1}{54}$
$\frac{4}{3}$	1	0	0					$-\frac{4}{61}$	$\frac{49}{183}$	$\frac{1}{3}$	$\frac{1}{3}$

		<b>3</b>	<b>6</b>	<b>15<sub>1</sub></b>	<b>15<sub>2</sub></b>	<b>24</b>	<b>42</b>	<b>15<sub>1</sub></b>	<b>15<sub>2</sub></b>	<b>15'</b>	<b>24</b>	<b>42</b>	<b>42</b>
<b>15 <math>\otimes</math> 8</b>	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$
$\frac{1}{3}$	$\frac{1}{2}$	0	0	$-\frac{9}{80}$	$-\frac{3}{40}$	$-\frac{121}{976}$	$\frac{4}{183}$	$\frac{2}{15}$	$\frac{8}{15}$				
$-\frac{2}{3}$	0	1	$\frac{1}{2}$	$\frac{1}{40}$	$\frac{3}{20}$	$-\frac{9}{488}$	$-\frac{150}{549}$	$-\frac{4}{15}$	$\frac{4}{15}$				
$\frac{4}{3}$	1	-1	$\frac{1}{2}$	$\frac{3}{10}$	$\frac{1}{5}$	$\frac{3}{122}$	$\frac{200}{549}$	$\frac{1}{45}$	$\frac{4}{45}$	$-\frac{24}{61}$	$\frac{529}{4392}$	$-\frac{1}{8}$	$\frac{2}{9}$
$-\frac{2}{3}$	1	1	$\frac{1}{2}$	$-\frac{3}{20}$	$\frac{1}{10}$	$-\frac{75}{224}$	$\frac{121}{549}$	$-\frac{8}{45}$	$-\frac{2}{45}$	$-\frac{12}{61}$	$-\frac{361}{2196}$	$\frac{1}{4}$	$-\frac{1}{9}$
$\frac{1}{3}$	$\frac{1}{2}$	0	1	$-\frac{1}{80}$	$-\frac{5}{24}$	$\frac{225}{976}$	$\frac{196}{1647}$	$-\frac{10}{27}$	$\frac{8}{135}$	$\frac{9}{61}$	$-\frac{1}{1647}$	$-\frac{1}{3}$	$-\frac{4}{27}$
$\frac{1}{3}$	$\frac{3}{2}$	0	1	$\frac{2}{5}$	$-\frac{4}{15}$	$-\frac{18}{61}$	$\frac{2}{1647}$	$-\frac{4}{135}$	$-\frac{1}{135}$	0	$\frac{305}{432}$	$\frac{5}{48}$	$-\frac{5}{27}$
$\frac{1}{3}$	$\frac{3}{2}$	0	0							$\frac{16}{61}$	$\frac{25}{2928}$	$\frac{3}{16}$	$\frac{1}{3}$

		<b>3</b>	<b>15<sub>1</sub></b>	<b>15<sub>2</sub></b>	<b>42</b>	<b>6</b>	<b>15<sub>1</sub></b>	<b>15<sub>2</sub></b>	<b>15'</b>	<b>24</b>	<b>42</b>	<b>24</b>	<b>42</b>
<b>15 <math>\otimes</math> 8</b>	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$
	0	0	0	0	1	1	1	1	1	1	1	2	2
$-\frac{2}{3}$	0	0	0	$-\frac{3}{20}$	$-\frac{49}{244}$	$-\frac{3}{61}$	$\frac{3}{5}$						
$-\frac{5}{3}$	$\frac{1}{2}$	1	$\frac{1}{2}$	$-\frac{2}{5}$	$-\frac{6}{61}$	$\frac{49}{122}$	$-\frac{1}{10}$	$\frac{4}{15}$	$-\frac{12}{61}$	$-\frac{361}{2196}$	$\frac{1}{12}$	$-\frac{8}{45}$	$\frac{1}{9}$
$\frac{1}{3}$	$\frac{1}{2}$	-1	$\frac{1}{2}$	$\frac{3}{20}$	$\frac{9}{244}$	$\frac{100}{183}$	$\frac{4}{15}$	$\frac{1}{90}$	$-\frac{25}{122}$	$\frac{242}{1647}$	$-\frac{2}{9}$	$\frac{16}{135}$	$\frac{8}{27}$
$-\frac{2}{3}$	1	0	1	$\frac{3}{10}$	$-\frac{81}{122}$	$\frac{1}{366}$	$-\frac{1}{30}$	$-\frac{2}{15}$	$-\frac{6}{61}$	$\frac{49}{122}$	$\frac{1}{6}$	$-\frac{1}{5}$	0
$\frac{1}{3}$	$\frac{3}{2}$	-1	$\frac{1}{2}$					$\frac{16}{45}$	$\frac{16}{61}$	$\frac{361}{1647}$	$\frac{1}{9}$	$\frac{2}{135}$	$\frac{1}{27}$
$-\frac{2}{3}$	1	0	0					$-\frac{1}{5}$	$\frac{1}{61}$	$-\frac{49}{732}$	$\frac{1}{4}$	$\frac{2}{15}$	$\frac{1}{3}$
$-\frac{2}{3}$	0	0	1					$-\frac{1}{30}$	$\frac{27}{122}$	$-\frac{1}{1098}$	$-\frac{1}{6}$	$-\frac{16}{45}$	$\frac{2}{9}$

		<b>15</b>	<b>15</b>	<b>15'</b>	<b>42</b>	<b>24</b>	<b>42</b>	<b>15'</b>	<b>42</b>
<b>15</b>	<b>⊗</b>	<b>8</b>	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0
									1
									1
									1
									1

Table 21: Isoscalar factors for **15**  $\otimes$  **10**.

		<b>24</b>	<b>42</b>	<b>48</b>	<b>6</b>	<b>24</b>	<b>15</b>	<b>24</b>	<b>42</b>	<b>15'</b>	<b>42</b>	<b>48</b>	<b>48</b>
<b>15</b>	<b>⊗</b>	<b>10</b>	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$							
			$\frac{1}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	0	0	1	1	1	2	2	3

		<b>6</b>	<b>15</b>	<b>24</b>	<b>42</b>	<b>15</b>	<b>15'</b>	<b>24</b>	<b>42</b>	<b>48</b>	<b>42</b>	<b>48</b>	
<b>15</b>	<b>⊗</b>	<b>10</b>	$\frac{1}{3}$										
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$

		<b>15</b>	<b>42</b>	<b>6</b>	<b>15</b>	<b>15'</b>	<b>24</b>	<b>42</b>	<b>48</b>	<b>24</b>	<b>42</b>	<b>48</b>	
<b>15</b>	<b>⊗</b>	<b>10</b>	$-\frac{2}{3}$										
			0	0	1	1	1	1	1	2	2	2	

$15 \otimes 10$	$15 \quad 15' \quad 42 \quad 48 \quad 24 \quad 42 \quad 48 \quad 15' \quad 48 \quad 42 \quad 48 \quad 48 \quad 48$
$\frac{1}{2}$	$-\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{11}{3}$
$\frac{1}{2}$	$\frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad 0 \quad 0 \quad 1 \quad 1 \quad \frac{1}{2}$
$\frac{1}{3} \quad \frac{1}{2} \quad -2 \quad 0$	$\frac{1}{4} \quad \frac{9}{28} \quad \frac{1}{5} \quad \frac{8}{35}$
$-\frac{2}{3} \quad 0 \quad -1 \quad \frac{1}{2}$	$-\frac{1}{4} \quad \frac{1}{28} \quad -\frac{1}{5} \quad \frac{18}{35}$
$-\frac{2}{3} \quad 1 \quad -1 \quad \frac{1}{2}$	$\frac{1}{6} \quad \frac{3}{14} \quad -\frac{8}{15} \quad -\frac{3}{35}$
$-\frac{5}{3} \quad \frac{1}{2} \quad 0 \quad 1$	$-\frac{1}{3} \quad \frac{1}{15} \quad \frac{3}{5}$
$\frac{1}{3} \quad \frac{3}{2} \quad -2 \quad 0$	$\frac{1}{6} \quad -\frac{8}{15} \quad \frac{3}{10}$
$-\frac{2}{3} \quad 0 \quad -2 \quad 0$	$\frac{1}{2} \quad \frac{2}{5} \quad \frac{1}{10}$
$-\frac{5}{3} \quad \frac{1}{2} \quad -1 \quad \frac{1}{2}$	$\frac{3}{7} \quad \frac{4}{7}$
$-\frac{2}{3} \quad 1 \quad -2 \quad 0$	$\frac{4}{7} \quad -\frac{3}{7}$
$-\frac{5}{3} \quad \frac{1}{2} \quad -2 \quad 0$	$-\frac{2}{5} \quad \frac{3}{5}$
	$\frac{3}{5} \quad \frac{2}{5}$
	1

Table 22: Isoscalar factors for  $15' \otimes 3$ .

$15' \otimes 3$	$24 \quad 21 \quad 24 \quad 24 \quad 21 \quad 24 \quad 24 \quad 21 \quad 24 \quad 24 \quad 21 \quad 24 \quad 21 \quad 24 \quad 21 \quad 21$
$\frac{5}{3} \quad \frac{5}{3} \quad \frac{2}{3} \quad \frac{2}{3} \quad \frac{2}{3} \quad -\frac{1}{3} \quad -\frac{1}{3} \quad -\frac{1}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{7}{3} \quad -\frac{7}{3} \quad -\frac{10}{3}$	
$\frac{3}{2} \quad \frac{5}{2} \quad 1 \quad 2 \quad 2 \quad \frac{1}{2} \quad \frac{3}{2} \quad \frac{3}{2} \quad 0 \quad 1 \quad 1 \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad 0$	
$\frac{4}{3} \quad 2 \quad \frac{1}{3} \quad \frac{1}{2}$	-1
$\frac{1}{3} \quad \frac{3}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	1
$\frac{4}{3} \quad 2 \quad -\frac{2}{3} \quad 0$	
$-\frac{2}{3} \quad 1 \quad \frac{1}{3} \quad \frac{1}{2}$	
$\frac{1}{3} \quad \frac{3}{2} \quad -\frac{2}{3} \quad 0$	
$-\frac{5}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	
$-\frac{2}{3} \quad 1 \quad -\frac{2}{3} \quad 0$	
$-\frac{5}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 0$	
$-\frac{8}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$	
$-\frac{8}{3} \quad 0 \quad -\frac{2}{3} \quad 0$	
	1

Table 23: Isoscalar factors for  $\mathbf{15}' \otimes \overline{\mathbf{3}}$ .

$\mathbf{15}' \otimes \overline{\mathbf{3}}$	35	10	35	35	10	35	35	10	35	35	10	35	35	35
	2	1	1	1	0	0	0	-1	-1	-1	-2	-2	-2	-3
	2	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	0	0	1	$\frac{1}{2}$
$\frac{4}{3}$	2	$\frac{2}{3}$	0	1										
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{2}{3}$	0		$-\frac{1}{6}$	$\frac{5}{6}$								
$\frac{4}{3}$	2	$-\frac{1}{3}$	$\frac{1}{2}$		$\frac{5}{6}$	$\frac{1}{6}$	1							
$-\frac{2}{3}$	1	$\frac{2}{3}$	0				$-\frac{1}{3}$	$\frac{2}{3}$						
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$				$\frac{2}{3}$	$\frac{1}{3}$	1					
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	0						$-\frac{1}{2}$	$\frac{1}{2}$				
$-\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$						$\frac{1}{2}$	$\frac{1}{2}$	1			
$-\frac{8}{3}$	0	$\frac{2}{3}$	0								$-\frac{2}{3}$	$\frac{1}{3}$		1
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$								$\frac{1}{3}$	$\frac{2}{3}$		
$-\frac{8}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$											1

 Table 24: Isoscalar factors for  $\mathbf{15}' \otimes \mathbf{6}$ .

$\mathbf{15}' \otimes \mathbf{6}$	27	35	28	27	27	35	35	28	27	27	35	27	35	28
	2	2	2	1	1	1	1	1	0	0	0	0	0	0
	1	2	3	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	0	1	1	2	2	2
$\frac{4}{3}$	2	$\frac{2}{3}$	1	1	-1	1								
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{2}{3}$	1			1	$\frac{1}{4}$	$-\frac{3}{4}$	$-\frac{1}{3}$	$\frac{2}{3}$				
$\frac{4}{3}$	2	$-\frac{1}{3}$	$\frac{1}{2}$				$-\frac{3}{4}$	$-\frac{1}{4}$	$\frac{2}{3}$	$\frac{1}{3}$				
$-\frac{2}{3}$	1	$\frac{2}{3}$	1						1		$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{10}$	$-\frac{1}{2}$
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$							$-\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{3}{10}$	$\frac{1}{6}$	$\frac{8}{15}$
$\frac{4}{3}$	2	$-\frac{4}{3}$	0									$\frac{3}{5}$	$\frac{1}{3}$	$\frac{1}{15}$

$15' \otimes 6$	27 35 27 35 28 35 27 35 28 35 28 28
-1 -1 -1 -1 -1 -2 -2 -2 -2 -3 -3 -4	
$\frac{1}{2} \frac{1}{2} \frac{3}{2} \frac{3}{2} \frac{3}{2} 0 1 1 1 \frac{1}{2} \frac{1}{2} 0$	
$\frac{2}{3} 1 -\frac{1}{3} \frac{1}{2} -\frac{1}{4} -\frac{3}{4} -\frac{2}{5} 0 \frac{3}{5}$	
$-\frac{5}{3} \frac{1}{2} \frac{2}{3} 1 \frac{3}{4} -\frac{1}{4} \frac{3}{10} -\frac{1}{2} \frac{1}{5}$	
$\frac{1}{3} \frac{3}{2} -\frac{4}{3} 0 \frac{3}{10} \frac{1}{2} \frac{1}{5}$	
$-\frac{5}{3} \frac{1}{2} -\frac{1}{3} \frac{1}{2} -1 -\frac{3}{10} -\frac{1}{6} \frac{8}{15}$	
$-\frac{2}{3} 1 -\frac{4}{3} 0 \frac{1}{10} \frac{1}{2} \frac{2}{5}$	
$-\frac{8}{3} 0 \frac{2}{3} 1 \frac{3}{5} -\frac{1}{3} \frac{1}{15}$	
$-\frac{5}{3} \frac{1}{2} -\frac{4}{3} 0 \frac{1}{3} \frac{2}{3}$	
$-\frac{8}{3} 0 -\frac{1}{3} \frac{1}{2} -\frac{2}{3} \frac{1}{3}$	
$-\frac{8}{3} 0 -\frac{4}{3} 0 1$	

Table 25: Isoscalar factors for  $15' \otimes \bar{6}$ .

$15' \otimes \bar{6}$	60 24 60 60 6 24 60 24 60 60
$\frac{8}{3} \frac{5}{3} \frac{5}{3} \frac{5}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	
$2 \frac{3}{2} \frac{3}{2} \frac{5}{2} 1 1 1 2 2 3$	
$\frac{4}{3} 2 \frac{4}{3} 0 1$	
$\frac{1}{3} \frac{3}{2} \frac{4}{3} 0 -\frac{2}{7} \frac{5}{7}$	
$\frac{4}{3} 2 \frac{1}{3} \frac{1}{2} \frac{5}{7} \frac{2}{7} 1$	
$-\frac{2}{3} 1 \frac{4}{3} 0 \frac{1}{15} -\frac{16}{35} \frac{10}{21}$	
$\frac{1}{3} \frac{3}{2} \frac{1}{3} \frac{1}{2} -\frac{4}{15} \frac{9}{35} \frac{10}{21} -\frac{1}{7} \frac{6}{7}$	
$\frac{4}{3} 2 -\frac{2}{3} 1 \frac{2}{3} \frac{2}{7} \frac{1}{21} \frac{6}{7} \frac{1}{7} 1$	

$15' \otimes \bar{6}$	6 24 60 24 60 60 6 24 60 24 60 60 24 60 60
$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{4}{3} -\frac{4}{3} -\frac{4}{3} -\frac{4}{3} -\frac{4}{3} -\frac{7}{3} -\frac{7}{3} -\frac{7}{3} -\frac{10}{3}$	
$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{3}{2} \frac{3}{2} \frac{5}{2} 0 0 0 1 1 2 \frac{1}{2} \frac{1}{2} \frac{3}{2} 1$	
$-\frac{5}{3} \frac{1}{2} \frac{4}{3} 0 \frac{1}{5} -\frac{18}{35} \frac{2}{7}$	
$-\frac{2}{3} 1 \frac{1}{3} \frac{1}{2} -\frac{2}{5} \frac{1}{35} \frac{4}{7} -\frac{2}{7} \frac{5}{7}$	
$\frac{1}{3} \frac{3}{2} -\frac{2}{3} 1 \frac{2}{5} \frac{16}{35} \frac{1}{7} \frac{5}{7} \frac{2}{7} 1$	
$-\frac{8}{3} 0 \frac{4}{3} 0 \frac{2}{5} -\frac{16}{35} \frac{1}{7}$	
$-\frac{5}{3} \frac{1}{2} \frac{1}{3} \frac{1}{2} -\frac{2}{5} -\frac{1}{35} \frac{4}{7} -\frac{3}{7} \frac{4}{7}$	
$-\frac{2}{3} 1 -\frac{2}{3} 1 \frac{1}{5} \frac{18}{35} \frac{2}{7} \frac{4}{7} \frac{3}{7} 1$	
$-\frac{8}{3} 0 \frac{1}{3} \frac{1}{2} -\frac{4}{7} \frac{3}{7}$	
$-\frac{5}{3} \frac{1}{2} -\frac{2}{3} 1 \frac{3}{7} \frac{4}{7} 1$	
$-\frac{8}{3} 0 -\frac{2}{3} 1 1$	

Table 26: Isoscalar factors for  $\mathbf{15}' \otimes \mathbf{8}$ .

$\mathbf{15}' \otimes \mathbf{8}$	42	48	15	42	$15'$	42	48	48	15	42	15	$15'$	42	48	42	48		
$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$		
$\frac{3}{2}$	$\frac{5}{2}$	1	1	2	2	2	3	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$		
$\frac{4}{3}$	2	1	$\frac{1}{2}$	-1	1													
$\frac{1}{3}$	$\frac{3}{2}$	1	$\frac{1}{2}$			$\frac{1}{6}$	$-\frac{5}{6}$	$-\frac{3}{14}$	$-\frac{1}{10}$	$\frac{24}{35}$								
$\frac{4}{3}$	2	0	1			$-\frac{5}{6}$	$-\frac{1}{6}$	$\frac{9}{14}$	$-\frac{3}{10}$	$\frac{2}{35}$								
$\frac{4}{3}$	2	0	0					$\frac{1}{7}$	$\frac{3}{5}$	$\frac{9}{35}$								
$-\frac{2}{3}$	1	1	$\frac{1}{2}$								$\frac{1}{3}$	$-\frac{2}{3}$	$\frac{1}{12}$	$-\frac{9}{28}$	$-\frac{1}{6}$	$\frac{3}{7}$		
$\frac{1}{3}$	$\frac{3}{2}$	0	1								$-\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{5}{48}$	$\frac{45}{112}$	$-\frac{49}{120}$	$\frac{3}{35}$	$-\frac{1}{5}$	$\frac{4}{5}$
$\frac{4}{3}$	2	-1	$\frac{1}{2}$										$\frac{5}{8}$	$\frac{15}{56}$	$\frac{1}{20}$	$\frac{2}{35}$	$\frac{4}{5}$	$\frac{1}{5}$
$\frac{1}{3}$	$\frac{3}{2}$	0	0										$-\frac{3}{16}$	$\frac{1}{112}$	$\frac{3}{8}$	$\frac{3}{7}$		

$\mathbf{15}' \otimes \mathbf{8}$	15	42	15	$15'$	42	48	42	48
$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$
0	0	1	1	1	1	1	2	2
$-\frac{5}{3}$	$\frac{1}{2}$	1	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{4}$	$-\frac{9}{28}$	$-\frac{1}{5}$
$-\frac{2}{3}$	1	0	1	$-\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{6}$	$\frac{3}{14}$	$-\frac{8}{15}$
$\frac{1}{3}$	$\frac{3}{2}$	-1	$\frac{1}{2}$			$\frac{1}{3}$	$\frac{3}{7}$	$\frac{1}{15}$
$-\frac{2}{3}$	1	0	0			$-\frac{1}{4}$	$-\frac{1}{28}$	$\frac{1}{5}$
							$\frac{18}{35}$	

$\mathbf{15}' \otimes \mathbf{8}$	15	$15'$	42	48	42	48	$15'$	48	42	48	48
$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{11}{3}$
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
$-\frac{5}{3}$	$\frac{1}{2}$	0	0	$-\frac{3}{16}$	$-\frac{25}{112}$	$\frac{3}{40}$	$\frac{18}{35}$				
$-\frac{8}{3}$	0	1	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{3}{14}$	$-\frac{1}{5}$	$\frac{3}{35}$				
$-\frac{2}{3}$	1	-1	$\frac{1}{2}$	$\frac{1}{8}$	$\frac{27}{56}$	$\frac{1}{20}$	$\frac{12}{35}$	$\frac{2}{5}$	$\frac{3}{5}$		
$-\frac{5}{3}$	$\frac{1}{2}$	0	1	$-\frac{3}{16}$	$-\frac{9}{112}$	$-\frac{27}{40}$	$\frac{2}{35}$	$-\frac{3}{5}$	$\frac{2}{5}$		
$-\frac{8}{3}$	0	0	0					$-\frac{4}{7}$	$\frac{3}{7}$		
$-\frac{5}{3}$	$\frac{1}{2}$	-1	$\frac{1}{2}$					$\frac{3}{7}$	$\frac{4}{7}$	$\frac{1}{5}$	$\frac{4}{5}$
$-\frac{8}{3}$	0	0	1					$-\frac{4}{5}$	$\frac{1}{5}$		
$-\frac{8}{3}$	0	-1	$\frac{1}{2}$								1

Table 27: Isoscalar factors for  $\mathbf{15}' \otimes \mathbf{10}$ .

$\mathbf{15}' \otimes \mathbf{10}$	24	42	48	36	24	24	42	42	48	48	36
	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$
	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{7}{2}$	0	1	1	2	2	3	3
	$\frac{4}{3}$	2	1	$\frac{3}{2}$	-1	1					
	$\frac{1}{3}$	$\frac{3}{2}$	1	$\frac{3}{2}$			-1	$-\frac{1}{3}$	$\frac{2}{3}$	$\frac{2}{5}$	$-\frac{3}{5}$
	$\frac{4}{3}$	2	0	1				$\frac{2}{3}$	$\frac{1}{3}$	$-\frac{3}{5}$	$-\frac{2}{5}$
								$\frac{2}{5}$	$-\frac{1}{5}$	$\frac{4}{7}$	$\frac{3}{7}$

$\mathbf{15}' \otimes \mathbf{10}$	24	42	24	42	48	42	48	36	42	24	42	48	24	42	48	36	
	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	0	1	1	1	1	2	2	2	
	$\frac{1}{3}$	$\frac{3}{2}$	0	1	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{1}{3}$	$-\frac{1}{15}$	$-\frac{3}{5}$	$-\frac{2}{5}$	$\frac{1}{35}$	$\frac{4}{7}$					
	$-\frac{2}{3}$	1	1	$\frac{3}{2}$	$-\frac{2}{3}$	$\frac{1}{3}$	$-\frac{1}{6}$	$\frac{8}{15}$	$-\frac{3}{10}$	$\frac{1}{5}$	$-\frac{18}{35}$	$\frac{2}{7}$					
	$\frac{4}{3}$	2	-1	$\frac{1}{2}$			$-\frac{1}{2}$	$-\frac{2}{5}$	$-\frac{1}{10}$	$\frac{2}{5}$	$\frac{16}{35}$	$\frac{1}{7}$					
	$-\frac{2}{3}$	1	0	1						1	$\frac{1}{3}$	$\frac{1}{15}$	$-\frac{3}{5}$	$\frac{1}{5}$	$-\frac{1}{5}$	$-\frac{3}{35}$	
	$\frac{1}{3}$	$\frac{3}{2}$	-1	$\frac{1}{2}$							$-\frac{1}{6}$	$-\frac{8}{15}$	$-\frac{3}{10}$	$-\frac{3}{10}$	0	$\frac{5}{14}$	
	$-\frac{5}{3}$	$\frac{1}{2}$	1	$\frac{3}{2}$							$-\frac{1}{2}$	$\frac{2}{5}$	$-\frac{1}{10}$	$\frac{1}{10}$	$\frac{2}{5}$	$-\frac{27}{70}$	
	$\frac{4}{3}$	2	-2	0								$\frac{2}{5}$	$\frac{2}{5}$	$\frac{6}{35}$	$\frac{1}{35}$		

$\mathbf{15}' \otimes \mathbf{10}$	42	48	24	42	48	36	48	42	48	36	48	36	36	36	36
	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{11}{3}$	$-\frac{11}{3}$	$-\frac{11}{3}$	$-\frac{14}{3}$	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0	
	$-\frac{2}{3}$	1	-1	$\frac{1}{2}$	$-\frac{2}{5}$	$-\frac{1}{5}$	$-\frac{1}{5}$	$\frac{3}{35}$	$\frac{18}{35}$						
	$-\frac{5}{3}$	$\frac{1}{2}$	0	1	$\frac{3}{5}$	$-\frac{2}{5}$	$\frac{3}{10}$	0	$-\frac{5}{14}$	$\frac{12}{35}$					
	$\frac{1}{3}$	$\frac{3}{2}$	-2	0			$\frac{1}{10}$	$\frac{2}{5}$	$\frac{27}{70}$	$\frac{4}{35}$					
	$-\frac{8}{3}$	0	1	$\frac{3}{2}$			$-\frac{2}{5}$	$\frac{2}{5}$	$-\frac{6}{35}$	$\frac{1}{35}$					
	$-\frac{5}{3}$	$\frac{1}{2}$	-1	$\frac{1}{2}$						-1	$-\frac{2}{5}$	$-\frac{1}{35}$	$\frac{4}{7}$		
	$-\frac{2}{3}$	1	-2	0							$\frac{1}{5}$	$\frac{18}{35}$	$\frac{2}{7}$		
	$-\frac{8}{3}$	0	0	1							$\frac{2}{5}$	$-\frac{16}{35}$	$\frac{1}{7}$		
	$-\frac{5}{3}$	$\frac{1}{2}$	-2	0								$\frac{3}{7}$	$\frac{4}{7}$		
	$-\frac{8}{3}$	0	-1	$\frac{1}{2}$								$-\frac{4}{7}$	$\frac{3}{7}$		
	$-\frac{8}{3}$	0	-2	0										1	

Table 28: Isoscalar factors for  $\mathbf{15}' \otimes \mathbf{15}'$ .

$\mathbf{15}' \otimes \mathbf{15}'$			$\overline{\mathbf{15}'}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{15}'}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$
			$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$
			0	1	2	3	4	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{7}{2}$	$\frac{7}{2}$
$\frac{4}{3}$	2	$\frac{4}{3}$	2	1	-1	1	-1	1							
$\frac{4}{3}$	2	$\frac{1}{3}$	$\frac{3}{2}$						$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{4}{3}$	2						$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$

  

$\mathbf{15}' \otimes \mathbf{15}'$			$\overline{\mathbf{42}}$	$\overline{\mathbf{15}'}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	
			$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
			0	1	1	1	2	2	2	3	3	3	
$\frac{1}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{3}{2}$	-1	$-\frac{1}{3}$	0	$\frac{2}{3}$	$\frac{2}{5}$	0	$-\frac{3}{5}$	$-\frac{3}{7}$	0	$\frac{4}{7}$
$\frac{4}{3}$	2	$-\frac{2}{3}$	1		$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{6}$	$-\frac{3}{10}$	$-\frac{1}{2}$	$-\frac{1}{5}$	$\frac{2}{7}$	$\frac{1}{2}$	$\frac{3}{14}$
$-\frac{2}{3}$	1	$\frac{4}{3}$	2		$\frac{1}{3}$	$-\frac{1}{2}$	$\frac{1}{6}$	$-\frac{3}{10}$	$\frac{1}{2}$	$-\frac{1}{5}$	$\frac{2}{7}$	$-\frac{1}{2}$	$\frac{3}{14}$

  

$\mathbf{15}' \otimes \mathbf{15}'$			$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{15}'}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	
			$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{2}{3}$	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{20}$	$-\frac{1}{4}$	$-\frac{9}{20}$	$-\frac{3}{10}$	$-\frac{1}{14}$	$\frac{1}{5}$	$\frac{3}{7}$
$-\frac{2}{3}$	1	$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{4}$	$\frac{1}{20}$	$\frac{1}{4}$	$-\frac{9}{20}$	$\frac{3}{10}$	$-\frac{1}{14}$	$-\frac{1}{5}$	$\frac{3}{7}$
$\frac{4}{3}$	2	$-\frac{5}{3}$	$\frac{1}{2}$			$-\frac{1}{4}$	$-\frac{9}{20}$	$-\frac{1}{4}$	$-\frac{1}{20}$	$\frac{1}{5}$	$\frac{3}{7}$	$\frac{3}{10}$	$\frac{1}{14}$
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{4}{3}$	2			$\frac{1}{4}$	$-\frac{9}{20}$	$\frac{1}{4}$	$-\frac{1}{20}$	$-\frac{1}{5}$	$\frac{3}{7}$	$-\frac{3}{10}$	$\frac{1}{14}$

  

$\mathbf{15}' \otimes \mathbf{15}'$			$\overline{\mathbf{60}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{15}'}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	
			$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	
			0	1	1	1	2	2	2	2	2	
$-\frac{2}{3}$	1	$-\frac{2}{3}$	1	1	$\frac{2}{5}$	0	$-\frac{3}{5}$	$\frac{1}{5}$	0	$-\frac{2}{7}$	0	$\frac{18}{35}$
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{5}{3}$	$\frac{1}{2}$		$-\frac{3}{10}$	$-\frac{1}{2}$	$-\frac{1}{5}$	$-\frac{1}{5}$	$-\frac{1}{10}$	$\frac{1}{14}$	$\frac{2}{5}$	$\frac{8}{35}$
$-\frac{5}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{3}{2}$		$-\frac{3}{10}$	$\frac{1}{2}$	$-\frac{1}{5}$	$-\frac{1}{5}$	$\frac{1}{10}$	$\frac{1}{14}$	$-\frac{2}{5}$	$\frac{8}{35}$
$\frac{4}{3}$	2	$-\frac{8}{3}$	0					$\frac{1}{5}$	$\frac{2}{5}$	$\frac{2}{7}$	$\frac{1}{10}$	$\frac{1}{70}$
$-\frac{8}{3}$	0	$\frac{4}{3}$	2					$\frac{1}{5}$	$-\frac{2}{5}$	$\frac{2}{7}$	$-\frac{1}{10}$	$\frac{1}{70}$

$15' \otimes 15'$	$\overline{60}$	$\overline{63}$	$\overline{42}$	$\overline{60}$	$\overline{63}$	$\overline{45}$	$\overline{63}$	$\overline{60}$	$\overline{63}$	$\overline{45}$	$\overline{63}$	$\overline{45}$	$\overline{45}$
	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{13}{3}$	$-\frac{13}{3}$	$-\frac{16}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$0$	$1$	$1$	$1$	$\frac{1}{2}$	$\frac{1}{2}$	$0$
$-\frac{2}{3}$	$1$	$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{3}{10}$	$-\frac{1}{14}$	$\frac{1}{5}$	$\frac{3}{7}$				
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	$1$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{3}{10}$	$-\frac{1}{14}$	$-\frac{1}{5}$	$\frac{3}{7}$				
$\frac{1}{3}$	$\frac{3}{2}$	$-\frac{8}{3}$	$0$			$\frac{1}{5}$	$\frac{3}{7}$	$\frac{3}{10}$	$\frac{1}{14}$				
$-\frac{8}{3}$	$0$	$\frac{1}{3}$	$\frac{3}{2}$			$-\frac{1}{5}$	$\frac{3}{7}$	$-\frac{3}{10}$	$\frac{1}{14}$				
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{5}{3}$	$\frac{1}{2}$							$-1$	$-\frac{3}{7}$	$0$	$\frac{4}{7}$
$-\frac{2}{3}$	$1$	$-\frac{8}{3}$	$0$								$\frac{2}{7}$	$\frac{1}{2}$	$\frac{3}{14}$
$-\frac{8}{3}$	$0$	$-\frac{2}{3}$	$1$								$\frac{2}{7}$	$-\frac{1}{2}$	$\frac{3}{14}$
$-\frac{5}{3}$	$\frac{1}{2}$	$-\frac{8}{3}$	$0$									$\frac{1}{2}$	$\frac{1}{2}$
$-\frac{8}{3}$	$0$	$-\frac{5}{3}$	$\frac{1}{2}$									$-\frac{1}{2}$	$\frac{1}{2}$
$-\frac{8}{3}$	$0$	$-\frac{8}{3}$	$0$										$1$

Table 29: Isoscalar factors for  $\overline{\mathbf{21}} \otimes \mathbf{3}$ .

$\overline{\mathbf{21}} \otimes \mathbf{3}$	$35$	$28$	$35$	$35$	$28$	$35$	$35$	$28$	$35$	$35$	$28$	$35$	$28$	$28$		
	$2$	$2$	$1$	$1$	$1$	$0$	$0$	$0$	$-1$	$-1$	$-1$	$-2$	$-2$	$-3$	$-4$	
	$2$	$3$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$1$	$2$	$2$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$0$	$1$	$1$	$\frac{1}{2}$	$\frac{1}{2}$
$\frac{5}{3}$	$\frac{5}{2}$	$\frac{1}{3}$	$\frac{1}{2}$			$-1$	$1$									
$\frac{2}{3}$	$2$	$\frac{1}{3}$	$\frac{1}{2}$				$-1$	$-\frac{1}{6}$	$\frac{5}{6}$							
$\frac{5}{3}$	$\frac{5}{2}$	$-\frac{2}{3}$	$0$					$\frac{5}{6}$	$\frac{1}{6}$							
$-\frac{1}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$					$-1$	$-\frac{1}{3}$	$\frac{2}{3}$						
$\frac{2}{3}$	$2$	$-\frac{2}{3}$	$0$						$\frac{2}{3}$	$\frac{1}{3}$						
$-\frac{4}{3}$	$1$	$\frac{1}{3}$	$\frac{1}{2}$						$-1$	$-\frac{1}{2}$	$\frac{1}{2}$					
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{2}{3}$	$0$							$\frac{1}{2}$	$\frac{1}{2}$					
$-\frac{7}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$							$-1$	$-\frac{2}{3}$	$\frac{1}{3}$				
$-\frac{4}{3}$	$1$	$-\frac{2}{3}$	$0$								$\frac{1}{3}$	$\frac{2}{3}$				
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	$0$								$\frac{1}{6}$	$\frac{5}{6}$				
$-\frac{10}{3}$	$0$	$\frac{1}{3}$	$\frac{1}{2}$								$-\frac{5}{6}$	$\frac{1}{6}$				
$-\frac{10}{3}$	$0$	$-\frac{2}{3}$	$0$												$1$	

Table 30: Isoscalar factors for  $\overline{\mathbf{21}} \otimes \overline{\mathbf{3}}$ .

$\overline{\mathbf{21}} \otimes \overline{\mathbf{3}}$	48 15' 48 48 15' 48 48 15' 48 48 15' 48 48 15' 48 48 15' 48 48 48
$\frac{7}{3}$	$\frac{4}{3} \quad \frac{4}{3} \quad \frac{4}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad -\frac{2}{3} \quad -\frac{2}{3} \quad -\frac{2}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{5}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{8}{3} \quad -\frac{11}{3}$
$\frac{5}{2}$	$2 \quad 2 \quad 3 \quad \frac{3}{2} \quad \frac{3}{2} \quad \frac{5}{2} \quad 1 \quad 1 \quad 2 \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{3}{2} \quad 0 \quad 0 \quad 1 \quad \frac{1}{2}$
$\frac{5}{3}$	0
$\frac{2}{3}$	1
$\frac{5}{3}$	$-\frac{1}{7} \quad \frac{6}{7}$
$\frac{5}{3}$	1
$-\frac{1}{3}$	$-\frac{2}{7} \quad \frac{5}{7}$
$\frac{1}{3}$	1
$\frac{2}{3}$	$-\frac{3}{7} \quad \frac{4}{7}$
$\frac{4}{3}$	1
$-\frac{1}{3}$	$\frac{4}{7} \quad \frac{3}{7}$
$-\frac{7}{3}$	1
$-\frac{4}{3}$	$-\frac{4}{7} \quad \frac{3}{7}$
$-\frac{10}{3}$	1
$-\frac{7}{3}$	$\frac{3}{7} \quad \frac{4}{7}$
$-\frac{10}{3}$	1
	1

 Table 31: Isoscalar factors for  $\overline{\mathbf{21}} \otimes \mathbf{6}$ .

$\overline{\mathbf{21}} \otimes \mathbf{6}$	42 48 36 42 42 48 48 36 42 42 48 42 48 36
$\frac{7}{3}$	$\frac{7}{3} \quad \frac{7}{3} \quad \frac{7}{3} \quad \frac{4}{3} \quad \frac{4}{3} \quad \frac{4}{3} \quad \frac{4}{3} \quad \frac{4}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3} \quad \frac{1}{3}$
$\frac{3}{2}$	$\frac{5}{2} \quad \frac{7}{2} \quad \frac{7}{2} \quad 1 \quad 2 \quad 2 \quad 3 \quad 3 \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{5}{2} \quad \frac{5}{2} \quad \frac{5}{2}$
$\frac{5}{3}$	1
$\frac{2}{3}$	1
$\frac{5}{3}$	$1 \quad \frac{1}{5} \quad -\frac{4}{5} \quad -\frac{2}{7} \quad \frac{5}{7}$
$\frac{5}{3}$	$-\frac{4}{5} \quad -\frac{1}{5} \quad \frac{5}{7} \quad \frac{2}{7}$
$-\frac{1}{3}$	1
$\frac{2}{3}$	$1 \quad \frac{2}{5} \quad -\frac{3}{5} \quad \frac{1}{15} \quad -\frac{16}{35} \quad \frac{10}{21}$
$\frac{5}{3}$	$-\frac{3}{5} \quad -\frac{2}{5} \quad -\frac{4}{15} \quad \frac{9}{35} \quad \frac{10}{21}$
$\frac{5}{3}$	$\frac{2}{3} \quad \frac{2}{7} \quad \frac{2}{21}$
	0

$\overline{21} \otimes 6$	42	42	48	42	48	36	42	48	42	48	36	48	42	48	36	48	36	36
	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{11}{3}$	$-\frac{11}{3}$	$-\frac{14}{3}$			
	0	1	1	2	2	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	0
$-\frac{4}{3}$	1	$\frac{2}{3}$	1	1	$\frac{3}{5}$	$-\frac{2}{5}$	$\frac{1}{5}$	$-\frac{18}{35}$	$\frac{2}{7}$									
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$		$-\frac{2}{5}$	$-\frac{3}{5}$	$-\frac{2}{5}$	$\frac{1}{35}$	$\frac{4}{7}$									
$\frac{2}{3}$	2	$-\frac{4}{3}$	0				$\frac{2}{5}$	$\frac{16}{35}$	$\frac{1}{7}$									
$-\frac{4}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$				$-\frac{1}{5}$	$-\frac{4}{5}$	$-\frac{2}{5}$	$-\frac{1}{35}$	$\frac{4}{7}$							
$-\frac{7}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1				$\frac{4}{5}$	$-\frac{1}{5}$	$\frac{2}{5}$	$-\frac{16}{35}$	$\frac{1}{7}$							
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{4}{3}$	0						$\frac{1}{5}$	$\frac{18}{35}$	$\frac{2}{7}$							
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$									-1	$-\frac{4}{15}$	$-\frac{9}{35}$	$\frac{10}{21}$			
$-\frac{4}{3}$	1	$-\frac{4}{3}$	0										$\frac{1}{15}$	$\frac{16}{35}$	$\frac{10}{21}$			
$-\frac{10}{3}$	0	$\frac{2}{3}$	1										$\frac{2}{3}$	$-\frac{2}{7}$	$\frac{1}{21}$			
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0													$\frac{2}{7}$	$\frac{5}{7}$	
$-\frac{10}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$													$-\frac{5}{7}$	$\frac{2}{7}$	
$-\frac{10}{3}$	0	$-\frac{4}{3}$	0															1

Table 32: Isoscalar factors for  $\overline{21} \otimes \overline{6}$ .

$\overline{21} \otimes \overline{6}$	81	35	81	81	10	35	81	35	81	81	10	35	81	35	81	81	81	
	3	2	2	2	1	1	1	1	1	1	1	0	0	0	0	0	0	
	$\frac{5}{2}$	2	2	3	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{7}{2}$	1	1	1	2	2	3		
$\frac{5}{3}$	$\frac{5}{2}$	$\frac{4}{3}$	0	1														
$\frac{2}{3}$	2	$\frac{2}{3}$	0		$-\frac{1}{4}$	$\frac{3}{4}$												
$\frac{5}{3}$	$\frac{5}{2}$	$\frac{1}{3}$	$\frac{1}{2}$		$\frac{3}{4}$	$\frac{1}{4}$	1											
$-\frac{1}{3}$	$\frac{3}{2}$	$\frac{4}{3}$	0				$\frac{1}{21}$	$-\frac{5}{12}$	$\frac{15}{28}$									
$\frac{2}{3}$	2	$\frac{1}{3}$	$\frac{1}{2}$				$-\frac{5}{21}$	$\frac{1}{3}$	$\frac{3}{7}$	$-\frac{1}{8}$	$\frac{7}{8}$							
$\frac{5}{3}$	$\frac{5}{2}$	$-\frac{2}{3}$	1				$\frac{5}{7}$	$\frac{1}{4}$	$\frac{1}{28}$	$\frac{7}{8}$	$\frac{1}{8}$	1						
$-\frac{4}{3}$	1	$\frac{4}{3}$	0										$\frac{1}{7}$	$-\frac{1}{2}$	$\frac{5}{14}$			
$-\frac{1}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$										$-\frac{8}{21}$	$\frac{1}{12}$	$\frac{15}{28}$	$-\frac{1}{4}$	$\frac{3}{4}$	1
$\frac{2}{3}$	2	$-\frac{2}{3}$	1										$\frac{10}{21}$	$\frac{5}{12}$	$\frac{3}{28}$	$\frac{3}{4}$	$\frac{1}{4}$	

$\overline{\mathbf{21}} \otimes \overline{\mathbf{6}}$	10 35 81 35 81 81 10 35 81 35 81 81 81 35 81 81 81	
-1 -1 -1 -1 -1 -1 -2 -2 -2 -2 -2 -2 -3 -3 -3 -4		
$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{3}{2} \frac{3}{2} \frac{5}{2} 0 0 0 1 1 2 \frac{1}{2} \frac{1}{2} \frac{3}{2} 1$		
$\frac{7}{3} \frac{1}{2} \frac{4}{3} 0$	$\frac{2}{7} -\frac{1}{2} \frac{3}{14}$	
$-\frac{4}{3} 1 \frac{1}{3} \frac{1}{2}$	$-\frac{3}{7} 0 \frac{4}{7} -\frac{3}{8} \frac{5}{8}$	
$-\frac{1}{3} \frac{3}{2} -\frac{2}{3} 1$	$\frac{2}{7} \frac{1}{2} \frac{3}{14} \frac{5}{8} \frac{3}{8}$	1
$-\frac{10}{3} 0 \frac{4}{3} 0$		$\frac{10}{21} -\frac{5}{12} \frac{3}{28}$
$-\frac{7}{3} \frac{1}{2} \frac{1}{3} \frac{1}{2}$		$-\frac{8}{21} -\frac{1}{12} \frac{15}{28}$
$-\frac{4}{3} 1 -\frac{2}{3} 1$		$\frac{1}{7} \frac{1}{2} \frac{5}{14} \frac{1}{2} \frac{1}{2}$
$-\frac{10}{3} 0 \frac{1}{3} \frac{1}{2}$		$-\frac{5}{8} \frac{3}{8} 1$
$-\frac{7}{3} \frac{1}{2} -\frac{2}{3} 1$		
$-\frac{10}{3} 0 -\frac{2}{3} 1$		1

Table 33: Isoscalar factors for  $\overline{\mathbf{21}} \otimes \mathbf{8}$ .

$\overline{\mathbf{21}} \otimes \mathbf{8}$	$\overline{\mathbf{60}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{60}} \quad \overline{\mathbf{21}} \quad \overline{\mathbf{60}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{60}} \quad \overline{\mathbf{24}} \quad \overline{\mathbf{21}} \quad \overline{\mathbf{60}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{60}} \quad \overline{\mathbf{63}}$	
$\frac{8}{3} \frac{8}{3} \frac{5}{3} \frac{5}{3} \frac{5}{3} \frac{5}{3} \frac{5}{3} \frac{5}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$		
2 3 $\frac{3}{2} \frac{3}{2} \frac{3}{2} \frac{5}{2} \frac{5}{2} \frac{5}{2} \frac{7}{2} 1 1 2 2 2 2 3 3$		
$\frac{5}{3} \frac{5}{2} 1 \frac{1}{2}$	-1 1	
$\frac{2}{3} 2 1 \frac{1}{2}$		$\frac{1}{7} -\frac{6}{7} -\frac{3}{16} -\frac{1}{12} \frac{35}{48}$
$\frac{5}{3} \frac{5}{2} 0 1$		$-\frac{6}{7} -\frac{1}{7} \frac{21}{32} -\frac{7}{24} \frac{5}{96}$
$\frac{5}{3} \frac{5}{2} 0 0$		$\frac{5}{32} \frac{5}{8} \frac{7}{32}$
$-\frac{1}{3} \frac{3}{2} 1 \frac{1}{2}$		$\frac{2}{7} -\frac{5}{7} \frac{2}{35} -\frac{3}{10} -\frac{1}{7} \frac{1}{2}$
$\frac{2}{3} 2 0 1$		$-\frac{5}{7} -\frac{2}{7} -\frac{3}{35} \frac{9}{20} -\frac{8}{21} \frac{1}{12}$
$\frac{5}{3} \frac{5}{2} -1 \frac{1}{2}$		$\frac{24}{35} \frac{9}{40} \frac{1}{21} \frac{1}{24}$
$\frac{2}{3} 2 0 0$		$-\frac{6}{35} \frac{1}{40} \frac{3}{7} \frac{3}{8}$

$\overline{\mathbf{21}} \otimes \mathbf{8}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$
$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$							
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$0$	$0$	$1$	$1$	$1$	$1$	$1$	$2$	
$-\frac{4}{3}$	$1$	$1$	$\frac{1}{2}$	$\frac{3}{7}$	$-\frac{4}{7}$	$\frac{6}{35}$	$-\frac{27}{80}$	$-\frac{5}{28}$	$\frac{5}{16}$							
$-\frac{1}{3}$	$\frac{3}{2}$	$0$	$1$	$-\frac{4}{7}$	$-\frac{3}{7}$	$-\frac{1}{7}$	$\frac{9}{32}$	$-\frac{27}{56}$	$\frac{3}{32}$	$-\frac{1}{3}$	$\frac{2}{3}$					
$\frac{2}{3}$	$2$	$-1$	$\frac{1}{2}$			$\frac{3}{7}$	$\frac{3}{8}$	$\frac{1}{14}$	$\frac{1}{8}$	$\frac{2}{3}$	$\frac{1}{3}$					
$-\frac{1}{3}$	$\frac{3}{2}$	$0$	$0$			$-\frac{9}{35}$	$-\frac{1}{160}$	$\frac{15}{56}$	$\frac{15}{32}$							
$-\frac{7}{3}$	$\frac{1}{2}$	$1$	$\frac{1}{2}$							$\frac{4}{7}$	$-\frac{3}{7}$	$\frac{12}{35}$	$-\frac{3}{10}$	$-\frac{4}{21}$	$\frac{1}{6}$	
$-\frac{4}{3}$	$1$	$0$	$1$							$-\frac{3}{7}$	$-\frac{4}{7}$	$-\frac{6}{35}$	$\frac{3}{20}$	$-\frac{25}{42}$	$\frac{1}{12}$	
$-\frac{1}{3}$	$\frac{3}{2}$	$-1$	$\frac{1}{2}$									$\frac{8}{35}$	$\frac{9}{20}$	$\frac{1}{14}$	$\frac{1}{4}$	
$-\frac{4}{3}$	$1$	$0$	$0$									$-\frac{9}{35}$	$-\frac{1}{10}$	$\frac{1}{7}$	$\frac{1}{2}$	

$\overline{\mathbf{21}} \otimes \mathbf{8}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{63}}$
$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{13}{3}$
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$0$	$0$	$1$	$1$	$1$	$\frac{1}{2}$
$-\frac{7}{3}$	$\frac{1}{2}$	$0$	$0$	$-\frac{6}{35}$	$-\frac{49}{160}$	$\frac{3}{56}$	$\frac{15}{32}$				
$-\frac{10}{3}$	$0$	$1$	$\frac{1}{2}$	$\frac{4}{7}$	$-\frac{3}{16}$	$-\frac{5}{28}$	$\frac{1}{16}$				
$-\frac{4}{3}$	$1$	$-1$	$\frac{1}{2}$	$\frac{3}{35}$	$\frac{9}{20}$	$\frac{1}{21}$	$\frac{5}{12}$	$\frac{1}{3}$	$\frac{2}{3}$		
$-\frac{7}{3}$	$\frac{1}{2}$	$0$	$1$	$-\frac{6}{35}$	$\frac{9}{160}$	$-\frac{121}{168}$	$\frac{5}{96}$	$-\frac{2}{3}$	$\frac{1}{3}$		
$-\frac{10}{3}$	$0$	$0$	$0$					$-\frac{5}{8}$	$\frac{3}{8}$		
$-\frac{7}{3}$	$\frac{1}{2}$	$-1$	$\frac{1}{2}$					$\frac{3}{8}$	$\frac{5}{8}$	$\frac{1}{6}$	$\frac{5}{6}$
$-\frac{10}{3}$	$0$	$0$	$1$					$-\frac{5}{6}$	$\frac{1}{6}$		
$-\frac{10}{3}$	$0$	$-1$	$\frac{1}{2}$								$1$

Table 34: Isoscalar factors for  $\overline{\mathbf{21}} \otimes \mathbf{10}$ .

$\overline{\mathbf{21}} \otimes \mathbf{10}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$
	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$						
	$1$	$2$	$3$	$4$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{7}{2}$	$\frac{7}{2}$
$\frac{5}{3}$	$\frac{5}{2}$	$1$	$\frac{3}{2}$		$-1$	$1$					
$\frac{2}{3}$	$2$	$1$	$\frac{3}{2}$				$-1$	$-\frac{1}{4}$	$\frac{3}{4}$	$\frac{1}{3}$	$-\frac{2}{3}$
$\frac{5}{3}$	$\frac{5}{2}$	$0$	$1$					$\frac{3}{4}$	$\frac{1}{4}$	$-\frac{2}{3}$	$-\frac{1}{3}$
									$\frac{5}{8}$	$\frac{3}{8}$	

$\bar{21} \otimes 10$	$42$	$42$	$60$	$42$	$60$	$63$	$60$	$63$	$45$
	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
	0	1	1	2	2	2	3	3	3
$-\frac{1}{3} \ 3 \ 2 \ 1 \ \frac{3}{2}$	-1	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{10}$	$\frac{1}{2}$	$-\frac{2}{5}$	$\frac{1}{7}$	$-\frac{1}{2}$	$\frac{5}{14}$
$\frac{2}{3} \ 2 \ 0 \ 1$		$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{10}$	$-\frac{1}{6}$	$-\frac{8}{15}$	$-\frac{8}{21}$	$\frac{1}{12}$	$\frac{15}{28}$
$\frac{5}{3} \ \frac{5}{2} \ -1 \ \frac{1}{2}$				$-\frac{3}{5}$	$-\frac{1}{3}$	$-\frac{1}{15}$	$\frac{10}{21}$	$\frac{5}{12}$	$\frac{3}{28}$

$\bar{21} \otimes 10$	$42$	$60$	$42$	$60$	$63$	$42$	$60$	$63$	$45$
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$
$-\frac{1}{3} \ 3 \ 2 \ 0 \ 1$	$\frac{1}{4}$	$\frac{3}{4}$	$\frac{2}{5}$	0	$-\frac{3}{5}$	$\frac{3}{20}$	$-\frac{25}{84}$	$-\frac{1}{60}$	$\frac{15}{28}$
$-\frac{4}{3} \ 1 \ 1 \ \frac{3}{2}$	$-\frac{3}{4}$	$\frac{1}{4}$	$-\frac{3}{10}$	$\frac{1}{2}$	$-\frac{1}{5}$	$-\frac{1}{20}$	$\frac{9}{28}$	$-\frac{9}{20}$	$\frac{5}{28}$
$\frac{2}{3} \ 2 \ -1 \ \frac{1}{2}$			$-\frac{3}{10}$	$-\frac{1}{2}$	$-\frac{1}{5}$	$-\frac{3}{10}$	$\frac{1}{42}$	$\frac{49}{120}$	$\frac{15}{56}$
$\frac{5}{3} \ \frac{5}{2} \ -2 \ 0$						$\frac{1}{2}$	$\frac{5}{14}$	$\frac{1}{8}$	$\frac{1}{56}$

$\bar{21} \otimes 10$	$60$	$42$	$60$	$63$	$42$	$60$	$63$	$45$
	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$
	0	1	1	1	2	2	2	2
$-\frac{4}{3} \ 1 \ 0 \ 1$	1	$\frac{3}{10}$	$\frac{1}{6}$	$-\frac{8}{15}$	$\frac{3}{10}$	$-\frac{1}{14}$	$-\frac{1}{5}$	$\frac{3}{7}$
$-\frac{1}{3} \ 3 \ 2 \ -1 \ \frac{1}{2}$		$-\frac{1}{10}$	$-\frac{1}{2}$	$-\frac{2}{5}$	$-\frac{3}{10}$	$-\frac{1}{14}$	$\frac{1}{5}$	$\frac{3}{7}$
$-\frac{7}{3} \ \frac{1}{2} \ 1 \ \frac{3}{2}$		$-\frac{3}{5}$	$\frac{1}{3}$	$-\frac{1}{15}$	$-\frac{1}{5}$	$\frac{3}{7}$	$-\frac{3}{10}$	$\frac{1}{14}$
$\frac{2}{3} \ 2 \ -2 \ 0$					$\frac{1}{5}$	$\frac{3}{7}$	$\frac{3}{10}$	$\frac{1}{14}$

$\bar{21} \otimes 10$	$60$	$63$	$42$	$60$	$63$	$45$	$63$	$60$	$63$	$45$	$63$	$45$	$45$
	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{13}{3}$	$-\frac{13}{3}$	$-\frac{16}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	0
$-\frac{4}{3} \ 1 \ -1 \ \frac{1}{2}$	$-\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{3}{20}$	$-\frac{25}{84}$	$\frac{1}{60}$	$\frac{15}{28}$							
$-\frac{7}{3} \ \frac{1}{2} \ 0 \ 1$	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{3}{10}$	$\frac{1}{42}$	$-\frac{49}{120}$	$\frac{15}{56}$							
$-\frac{1}{3} \ \frac{3}{2} \ -2 \ 0$			$\frac{1}{20}$	$\frac{9}{28}$	$\frac{9}{20}$	$\frac{5}{28}$							
$-\frac{10}{3} \ 0 \ 1 \ \frac{3}{2}$			$-\frac{1}{2}$	$\frac{5}{14}$	$-\frac{1}{8}$	$\frac{1}{56}$							
$-\frac{7}{3} \ \frac{1}{2} \ -1 \ \frac{1}{2}$							$-1$	$-\frac{8}{21}$	$-\frac{1}{12}$	$\frac{15}{28}$			
$-\frac{4}{3} \ 1 \ -2 \ 0$								$\frac{1}{7}$	$\frac{1}{2}$	$\frac{5}{14}$			
$-\frac{10}{3} \ 0 \ 0 \ 1$								$\frac{10}{21}$	$-\frac{5}{12}$	$\frac{3}{28}$			
$-\frac{7}{3} \ \frac{1}{2} \ -2 \ 0$											$\frac{3}{8}$	$\frac{5}{8}$	
$-\frac{10}{3} \ 0 \ -1 \ \frac{1}{2}$											$-\frac{5}{8}$	$\frac{3}{8}$	
$-\frac{10}{3} \ 0 \ -2 \ 0$													1

Table 35: Isoscalar factors for  $\overline{\mathbf{24}} \otimes \mathbf{3}$ .

	27	35	27	10	27	35	35	27	10	27	35	27	35
$\overline{\mathbf{24}} \otimes \mathbf{3}$	2	2	1	1	1	1	1	0	0	0	0	0	0
	1	2	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	0	1	1	1	2	2
$\frac{5}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$	-1	1								
$\frac{2}{3}$	1	$\frac{1}{3}$	$\frac{1}{2}$			-1	$-\frac{1}{16}$	$-\frac{5}{32}$	$\frac{25}{32}$				
$\frac{5}{3}$	$\frac{3}{2}$	$-\frac{2}{3}$	0				$\frac{5}{12}$	$\frac{3}{8}$	$\frac{5}{24}$				
$\frac{2}{3}$	2	$\frac{1}{3}$	$\frac{1}{2}$				$\frac{25}{48}$	$-\frac{15}{32}$	$-\frac{1}{96}$	1			
$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$							-1	$-\frac{1}{9}$	$-\frac{1}{3}$	$\frac{5}{9}$
$\frac{2}{3}$	1	$-\frac{2}{3}$	0								$\frac{1}{3}$	$\frac{1}{4}$	$\frac{5}{12}$
$-\frac{1}{3}$	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$								$\frac{5}{9}$	$-\frac{5}{12}$	$-\frac{1}{36}$
$\frac{2}{3}$	2	$-\frac{2}{3}$	0									$-\frac{1}{4}$	$\frac{3}{4}$
											$\frac{3}{4}$	$\frac{1}{4}$	

	10	27	35	27	35	10	35	27	35	35
$\overline{\mathbf{24}} \otimes \mathbf{3}$	-1	-1	-1	-1	-1	-2	-2	-2	-2	-3
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	0	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{5}{8}$				
$-\frac{4}{3}$	0	$\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{8}$	$-\frac{9}{16}$	$\frac{5}{16}$				
$-\frac{4}{3}$	1	$\frac{1}{3}$	$\frac{1}{2}$	$\frac{5}{8}$	$-\frac{5}{16}$	$-\frac{1}{16}$	$-\frac{1}{2}$	$\frac{1}{2}$		
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{2}{3}$	0				$\frac{1}{2}$	$\frac{1}{2}$		
$-\frac{4}{3}$	0	$-\frac{2}{3}$	0						$\frac{1}{6}$	$\frac{5}{6}$
$-\frac{7}{3}$	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$				$\frac{5}{6}$	$-\frac{1}{6}$	$-\frac{3}{4}$	$\frac{1}{4}$
$-\frac{4}{3}$	1	$-\frac{2}{3}$	0						$\frac{1}{4}$	$\frac{3}{4}$
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{2}{3}$	0							1

Table 36: Isoscalar factors for  $\overline{\mathbf{24}} \otimes \overline{\mathbf{3}}$ .

$\overline{\mathbf{24}} \otimes \overline{\mathbf{3}}$	42	15	42	15'	42	15	42	15	15'	42	42
$\frac{5}{3} \frac{3}{2} \frac{2}{3} 0$	1										
$\frac{2}{3} 1 \frac{2}{3} 0$		$-\frac{1}{6} \frac{5}{6}$									
$\frac{5}{3} \frac{3}{2} -\frac{1}{3} \frac{1}{2}$		$\frac{5}{6} \frac{1}{6}$		$-\frac{1}{2} \frac{1}{2}$							
$\frac{2}{3} 2 \frac{2}{3} 0$				$\frac{1}{2} \frac{1}{2}$							
$-\frac{1}{3} \frac{1}{2} \frac{2}{3} 0$					$-\frac{1}{3} \frac{2}{3}$						
$\frac{2}{3} 1 -\frac{1}{3} \frac{1}{2}$					$\frac{2}{3} \frac{1}{3}$		$\frac{1}{96} -\frac{15}{32} \frac{25}{48}$				
$-\frac{1}{3} \frac{3}{2} \frac{2}{3} 0$							$-\frac{5}{24} \frac{3}{8} \frac{5}{12}$				
$\frac{2}{3} 2 -\frac{1}{3} \frac{1}{2}$							$\frac{25}{32} \frac{5}{32} \frac{1}{16}$	1			

$\overline{\mathbf{24}} \otimes \overline{\mathbf{3}}$	15	42	15	15'	42	42	15	15'	42	42	15'	42
$-\frac{2}{3} -\frac{2}{3} -\frac{2}{3} -\frac{2}{3} -\frac{2}{3} -\frac{2}{3} -\frac{5}{3} -\frac{5}{3} -\frac{5}{3} -\frac{5}{3} -\frac{8}{3} -\frac{8}{3}$												
$0 0 1 1 1 2 \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{3}{2} 0 1$												
$-\frac{4}{3} 0 \frac{2}{3} 0$	$-\frac{1}{2} \frac{1}{2}$											
$-\frac{1}{3} \frac{1}{2} -\frac{1}{3} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2}$	$\frac{1}{36} -\frac{5}{12} \frac{5}{9}$										
$-\frac{4}{3} 1 \frac{2}{3} 0$		$-\frac{5}{12} \frac{1}{4} \frac{1}{3}$										
$-\frac{1}{3} \frac{3}{2} -\frac{1}{3} \frac{1}{2}$		$\frac{5}{9} \frac{1}{3} \frac{1}{9}$	1									
$-\frac{7}{3} \frac{1}{2} \frac{2}{3} 0$				$-\frac{5}{8} \frac{1}{8} \frac{1}{4}$								
$-\frac{4}{3} 0 -\frac{1}{3} \frac{1}{2}$				$\frac{1}{16} -\frac{5}{16} \frac{5}{8}$								
$-\frac{4}{3} 1 -\frac{1}{3} \frac{1}{2}$				$\frac{5}{16} \frac{9}{16} \frac{1}{8}$	1							
$-\frac{7}{3} \frac{1}{2} -\frac{1}{3} \frac{1}{2}$										1	1	

 Table 37: Isoscalar factors for  $\overline{\mathbf{24}} \otimes \mathbf{6}$ .

$\overline{\mathbf{24}} \otimes \mathbf{6}$	24	42	48	24	15	24	42	15'	42	48	48
$\frac{7}{3} \frac{7}{3} \frac{7}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3} \frac{4}{3}$											
$\frac{1}{2} \frac{3}{2} \frac{5}{2} 0 1 1 1 2 2 2 3$											
$\frac{5}{3} \frac{3}{2} \frac{2}{3} 1$	1	-1	1								
$\frac{2}{3} 1 \frac{2}{3} 1$				1	$\frac{1}{36} \frac{5}{18} -\frac{25}{36}$	$-\frac{3}{28} -\frac{1}{4} \frac{9}{14}$					
$\frac{5}{3} \frac{3}{2} -\frac{1}{3} \frac{1}{2}$					$-\frac{5}{18} -\frac{4}{9} -\frac{5}{18}$	$\frac{5}{14} \frac{3}{10} \frac{12}{35}$					
$\frac{2}{3} 2 \frac{2}{3} 1$					$-\frac{25}{36} \frac{5}{18} \frac{1}{36}$	$\frac{15}{28} -\frac{9}{20} -\frac{1}{70}$	1				

$\overline{24} \otimes 6$	15	24	42	15	15'	24	42	48	42	48
	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$
$\frac{2}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{2}{9}$	$-\frac{2}{9}$	$-\frac{5}{9}$	$-\frac{49}{288}$	$\frac{27}{224}$	$-\frac{5}{36}$	$\frac{5}{144}$
$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1	$\frac{1}{27}$	$\frac{16}{27}$	$-\frac{10}{27}$	$\frac{1}{27}$	$-\frac{1}{7}$	$\frac{5}{54}$	$-\frac{10}{27}$
$-\frac{1}{3}$	$\frac{3}{2}$	$\frac{2}{3}$	1	$-\frac{20}{27}$	$\frac{5}{27}$	$\frac{2}{27}$	$-\frac{25}{216}$	$\frac{25}{56}$	$\frac{5}{27}$	$-\frac{121}{540}$
$\frac{2}{3}$	2	$-\frac{1}{3}$	$\frac{1}{2}$				$\frac{25}{96}$	$\frac{25}{224}$	$-\frac{5}{12}$	$-\frac{49}{240}$
$\frac{5}{3}$	$\frac{3}{2}$	$-\frac{4}{3}$	0				$\frac{5}{12}$	$\frac{5}{28}$	$\frac{1}{6}$	$\frac{1}{14}$

$\overline{24} \otimes 6$	15	42	15	15'	24	42	48	24	42	48
	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$
	0	0	1	1	1	1	1	2	2	2
$\frac{2}{3}$	1	$-\frac{4}{3}$	0		$\frac{2}{9}$	$\frac{2}{7}$	$\frac{1}{18}$	$\frac{2}{9}$	$\frac{3}{14}$	
$-\frac{4}{3}$	0	$\frac{2}{3}$	1		$\frac{1}{12}$	$-\frac{3}{28}$	$\frac{1}{3}$	$-\frac{1}{3}$	$\frac{1}{7}$	
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{6}$	$-\frac{5}{6}$	$-\frac{25}{108}$	$\frac{1}{84}$	$-\frac{4}{27}$	$-\frac{1}{27}$	$\frac{4}{7}$
$-\frac{4}{3}$	1	$\frac{2}{3}$	1	$-\frac{5}{6}$	$\frac{1}{6}$	$-\frac{5}{18}$	$\frac{5}{14}$	$\frac{5}{18}$	$-\frac{2}{45}$	$-\frac{3}{70}$
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$			$\frac{5}{27}$	$\frac{5}{21}$	$-\frac{5}{27}$	$-\frac{49}{135}$	$-\frac{1}{35}$
$\frac{2}{3}$	2	$-\frac{4}{3}$	0						$\frac{1}{2}$	$\frac{2}{5}$

$\overline{24} \otimes 6$	15	15'	42	48	24	42	48	15'	48	42	48	48
	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{11}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	$\frac{1}{2}$
$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0	$\frac{1}{12}$	$\frac{9}{28}$	$\frac{1}{6}$	$\frac{3}{7}$					
$-\frac{4}{3}$	0	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{3}{16}$	$-\frac{1}{112}$	$-\frac{3}{8}$	$\frac{3}{7}$					
$-\frac{4}{3}$	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{5}{48}$	$\frac{45}{112}$	$-\frac{49}{120}$	$-\frac{3}{35}$	$-\frac{1}{3}$	$-\frac{1}{15}$	$\frac{3}{5}$		
$-\frac{7}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	1	$-\frac{5}{8}$	$\frac{15}{56}$	$\frac{1}{20}$	$-\frac{2}{35}$	$\frac{1}{2}$	$-\frac{2}{5}$	$\frac{1}{10}$		
$-\frac{1}{3}$	$\frac{3}{2}$	$-\frac{4}{3}$	0					$\frac{1}{6}$	$\frac{8}{15}$	$\frac{3}{10}$		
$-\frac{4}{3}$	0	$-\frac{4}{3}$	0					$\frac{2}{7}$	$\frac{5}{7}$			
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$					$\frac{5}{7}$	$-\frac{2}{7}$	$-\frac{3}{5}$	$\frac{2}{5}$	
$-\frac{4}{3}$	1	$-\frac{4}{3}$	0					$\frac{2}{5}$	$\frac{3}{5}$			
$-\frac{7}{3}$	$\frac{1}{2}$	$-\frac{4}{3}$	0									1

Table 38: Isoscalar factors for  $\overline{\mathbf{24}} \otimes \mathbf{8}$ .

$\overline{\mathbf{24}} \otimes \mathbf{8}$			$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{24}}_1$	$\overline{\mathbf{24}}_2$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$				
$\frac{5}{3} \frac{3}{2} 1 \frac{1}{2}$	-1	1														
$\frac{2}{3} 1 1 \frac{1}{2}$			$\frac{1}{6} -\frac{5}{6}$	$-\frac{1}{136} -\frac{625}{2856}$	$-\frac{5}{48} \frac{75}{112}$											
$\frac{5}{3} \frac{3}{2} 0 1$			$-\frac{5}{6} -\frac{1}{6}$	$\frac{25}{68} \frac{529}{1428}$	$-\frac{5}{24} \frac{3}{56}$											
$\frac{2}{3} 2 1 \frac{1}{2}$				$-\frac{75}{136} \frac{121}{952}$	$-\frac{5}{16} -\frac{1}{112}$											
$\frac{5}{3} \frac{3}{2} 0 0$				$-\frac{5}{68} \frac{135}{476}$	$\frac{3}{8} \frac{15}{56}$											
$\overline{\mathbf{24}} \otimes \mathbf{8}$			$\overline{\mathbf{15}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{6}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}_1$	$\overline{\mathbf{24}}_2$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}_1$	$\overline{\mathbf{24}}_2$	$\overline{\mathbf{21}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$
$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$	$\frac{2}{3} \frac{2}{3} \frac{2}{3} \frac{2}{3}$		
0 0 1 1	1 1 1 1	1 1 1 1	1 1 1 1	1 1 1 1	1 1 1 1	1 1 1 1	1 1 1 1	2 2 2 2	2 2 2 2	2 2 2 2	2 2 2 2	2 2 2 2	2 2 2 2	2 2 2 2	2 2 2 2	
$\frac{2}{3} 1 0 0$			$-\frac{1}{10} -\frac{1}{12} -\frac{9}{85} \frac{20}{357}$	$\frac{5}{24} \frac{25}{56}$												
$-\frac{1}{3} \frac{1}{2} 1 \frac{1}{2}$	$\frac{1}{3} -\frac{2}{3}$	$\frac{1}{45} \frac{2}{27} -\frac{8}{765} -\frac{1000}{3213}$	$-\frac{5}{27} \frac{25}{63}$													
$\frac{2}{3} 1 0 1$	$-\frac{2}{3} -\frac{1}{3}$	$-\frac{1}{60} -\frac{1}{8} \frac{24}{85} \frac{45}{238}$	$-\frac{5}{16} \frac{25}{336}$													
$\frac{5}{3} \frac{3}{2} -1 \frac{1}{2}$		$\frac{1}{3} \frac{5}{18} \frac{1}{102} \frac{625}{2142}$	$\frac{1}{36} \frac{5}{84}$													
$-\frac{1}{3} \frac{3}{2} 1 \frac{1}{2}$		$-\frac{1}{9} \frac{5}{54} \frac{121}{306} \frac{961}{6426}$	$-\frac{25}{108} -\frac{5}{252}$													
$\frac{2}{3} 2 0 1$		$\frac{5}{12} \frac{25}{72} -\frac{10}{51} \frac{5}{2142} -\frac{1}{144} -\frac{1}{336}$	$0 \frac{51}{70} \frac{3}{40} -\frac{3}{16} \frac{1}{112}$												1	
$\frac{2}{3} 2 0 0$								$\frac{5}{17} \frac{12}{595} \frac{3}{20} \frac{3}{8} \frac{9}{56}$								
$\overline{\mathbf{24}} \otimes \mathbf{8}$			$\overline{\mathbf{6}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}_1$	$\overline{\mathbf{24}}_2$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{15}}$	$\overline{\mathbf{24}}_1$	$\overline{\mathbf{24}}_2$	$\overline{\mathbf{21}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$
$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$	$-\frac{1}{3} -\frac{1}{3} -\frac{1}{3} -\frac{1}{3}$		
$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$	$\frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2}$		
$-\frac{1}{3} \frac{1}{2} 0 0$	$-\frac{3}{20} -\frac{1}{12} -\frac{49}{340} -\frac{5}{1428}$	$\frac{1}{12} \frac{15}{28}$														
$-\frac{4}{3} 0 1 \frac{1}{2}$	$\frac{1}{20} \frac{1}{4} -\frac{3}{340} -\frac{125}{476}$	$-\frac{1}{4} \frac{5}{28}$														
$-\frac{4}{3} 1 1 \frac{1}{2}$	$-\frac{1}{4} \frac{5}{36} -\frac{49}{204} \frac{841}{4284}$	$-\frac{5}{36} -\frac{1}{28}$														
$\frac{2}{3} 1 -1 \frac{1}{2}$	$\frac{1}{5} \frac{1}{9} \frac{4}{255} \frac{500}{1071}$	$\frac{1}{36} \frac{5}{28}$														
$-\frac{1}{3} \frac{1}{2} 0 1$	$-\frac{1}{60} -\frac{25}{108} \frac{529}{3060} \frac{845}{12852}$	$-\frac{49}{108} \frac{5}{84}$														
$-\frac{1}{3} \frac{3}{2} 0 1$	$\frac{1}{3} -\frac{5}{27} -\frac{64}{153} -\frac{16}{3213} -\frac{5}{108} -\frac{1}{84}$															
$\frac{2}{3} 2 -1 \frac{1}{2}$																
$-\frac{1}{3} \frac{3}{2} 0 0$								$-\frac{5}{24} \frac{5}{68} -\frac{121}{7140} \frac{9}{40} \frac{5}{24} \frac{15}{56}$								

$\overline{24} \otimes 8$	6	$\overline{24}_1$	$\overline{24}_2$	60	15	$\overline{24}_1$	$\overline{24}_2$	$\overline{21}$	42	60	42	60
	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$
	0	0	0	0	1	1	1	1	1	1	2	2
$-\frac{4}{3} 0 0 0$	$-\frac{3}{20}$	$-\frac{16}{85}$	$-\frac{15}{119}$	$\frac{15}{28}$								
$-\frac{7}{3} \frac{1}{2} 1 \frac{1}{2}$	$-\frac{1}{2}$	$-\frac{6}{68}$	$\frac{81}{238}$	$-\frac{1}{14}$	$\frac{5}{12}$	$-\frac{5}{34}$	$-\frac{529}{3570}$	$\frac{1}{20}$	$-\frac{1}{6}$	$\frac{1}{14}$		
$-\frac{1}{3} \frac{1}{2} -1 \frac{1}{2}$	$\frac{1}{10}$	$\frac{3}{170}$	$\frac{125}{238}$	$\frac{5}{14}$	$\frac{1}{108}$	$-\frac{49}{306}$	$\frac{841}{6426}$	$-\frac{1}{4}$	$\frac{5}{54}$	$\frac{5}{14}$		
$-\frac{4}{3} 1 0 1$	$\frac{1}{4}$	$-\frac{12}{17}$	$\frac{1}{119}$	$-\frac{1}{28}$	$-\frac{5}{36}$	$-\frac{10}{51}$	$\frac{224}{765}$	$\frac{3}{20}$	$-\frac{2}{9}$	0	$-\frac{1}{2}$	$\frac{1}{2}$
$-\frac{1}{3} \frac{3}{2} -1 \frac{1}{2}$					$\frac{5}{27}$	$\frac{40}{153}$	$\frac{4232}{16065}$	$\frac{1}{5}$	$\frac{54}{14}$	$\frac{1}{14}$	$\frac{1}{2}$	$\frac{1}{2}$
$-\frac{4}{3} 1 0 0$					$-\frac{5}{24}$	0	$-\frac{17}{105}$	$\frac{9}{40}$	$\frac{1}{12}$	$\frac{9}{28}$		
$-\frac{4}{3} 0 0 1$					$-\frac{1}{24}$	$\frac{4}{17}$	$-\frac{1}{357}$	$-\frac{1}{8}$	$-\frac{5}{12}$	$\frac{5}{28}$		
$\overline{24} \otimes 8$	$\overline{24}_1$	$\overline{24}_2$	$\overline{21}$	60	42	60	$\overline{21}$	60				
	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$			
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1				
$-\frac{7}{3} \frac{1}{2} 0 0$	$-\frac{5}{68}$	$\frac{1083}{2380}$	$\frac{3}{20}$	$\frac{9}{28}$								
$-\frac{4}{3} 0 -1 \frac{1}{2}$	$-\frac{3}{68}$	$\frac{81}{476}$	$-\frac{1}{4}$	$\frac{15}{28}$								
$-\frac{4}{3} 1 -1 \frac{1}{2}$	$\frac{15}{68}$	$\frac{529}{2380}$	$\frac{9}{20}$	$\frac{3}{28}$	$\frac{1}{4}$	$\frac{3}{4}$						
$-\frac{7}{3} \frac{1}{2} 0 1$	$-\frac{45}{68}$	$\frac{363}{2380}$	$\frac{3}{20}$	$-\frac{1}{28}$	$-\frac{3}{4}$	$\frac{1}{4}$						
$-\frac{7}{3} \frac{1}{2} -1 \frac{1}{2}$									1	1		

Table 39: Isoscalar factors for  $\mathbf{27} \otimes \mathbf{3}$ .

$\mathbf{27} \otimes \mathbf{3}$	24	42	24	15	24	42	42	15	24	42	15	24	42	42
	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$						
	$\frac{1}{2}$	$\frac{3}{2}$	0	1	1	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$
$2 1 \frac{1}{3} \frac{1}{2}$	-1	1												
$1 \frac{1}{2} \frac{1}{3} \frac{1}{2}$														
$2 1 -\frac{2}{3} 0$														
$1 \frac{3}{2} \frac{1}{3} \frac{1}{2}$														
$1 \frac{1}{2} -\frac{2}{3} 0$														
$0 0 \frac{1}{3} \frac{1}{2}$														
$0 1 \frac{1}{3} \frac{1}{2}$														
$1 \frac{3}{2} \frac{2}{3} 0$														
$0 2 \frac{1}{3} \frac{1}{2}$														1

$27 \otimes 3$		Isoscalar factors for $27 \otimes 3$													
		15	42	15	24	42	24	42	15	42	24	42	42	42	
		$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$		
		0	0	1	1	1	2	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	1		
0	0	$-\frac{2}{3}$	0	$\frac{1}{3}$	$\frac{2}{3}$										
-1	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{27}$	$-\frac{16}{27}$	$\frac{10}{27}$							
0	1	$-\frac{2}{3}$	0			$\frac{2}{9}$	$\frac{2}{9}$	$\frac{5}{9}$							
-1	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$			$\frac{20}{27}$	$-\frac{5}{27}$	$-\frac{2}{27}$	$-\frac{1}{3}$	$\frac{2}{3}$					
0	2	$-\frac{2}{3}$	0						$\frac{2}{3}$	$\frac{1}{3}$					
-1	$\frac{1}{2}$	$-\frac{2}{3}$	0								$\frac{1}{6}$	$\frac{5}{6}$			
-2	1	$\frac{1}{3}$	$\frac{1}{2}$						$\frac{5}{6}$	$-\frac{1}{6}$	$-\frac{2}{3}$	$\frac{1}{3}$			
-1	$\frac{3}{2}$	$-\frac{2}{3}$	0						$\frac{1}{3}$	$\frac{2}{3}$					
-2	1	$-\frac{2}{3}$	0											1	

Table 40: Isoscalar factors for  $27 \otimes 6$ .

$27 \otimes 6$		Isoscalar factors for $27 \otimes 6$									
		15'	42	60	15	15'	42	24	42	60	60
		$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$
		0	1	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$
2	1	$\frac{2}{3}$	1		1	-1	1				
2	1	$-\frac{1}{3}$	$\frac{1}{2}$				$-\frac{5}{12}$	$-\frac{1}{4}$	$-\frac{1}{3}$	$\frac{10}{21}$	$\frac{1}{6}$
1	$\frac{1}{2}$	$\frac{2}{3}$	1				$\frac{1}{36}$	$\frac{5}{12}$	$-\frac{5}{9}$	$-\frac{8}{63}$	$-\frac{5}{18}$
1	$\frac{3}{2}$	$\frac{2}{3}$	1				$-\frac{5}{9}$	$\frac{1}{3}$	$\frac{1}{9}$	$\frac{25}{63}$	$-\frac{5}{9}$
										$-\frac{1}{21}$	1

$27 \otimes 6$		Isoscalar factors for $27 \otimes 6$											
		15	42	6	15	15'	24	42	60	24	42	60	60
		$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
		0	0	1	1	1	1	1	1	2	2	2	3
1	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{8}{135}$	$-\frac{1}{6}$	$-\frac{5}{54}$	$\frac{16}{105}$	0	$\frac{100}{189}$		
0	1	$\frac{2}{3}$	1	$-\frac{2}{3}$	$\frac{1}{3}$	$-\frac{2}{45}$	$-\frac{1}{18}$	$\frac{5}{18}$	$\frac{121}{315}$	$-\frac{5}{36}$	$-\frac{25}{252}$	$-\frac{1}{21}$	$-\frac{5}{12}$
1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$			$\frac{8}{27}$	0	$-\frac{8}{27}$	$\frac{1}{21}$	$-\frac{1}{3}$	$-\frac{5}{189}$	$\frac{5}{21}$	$\frac{1}{3}$
0	2	$\frac{2}{3}$	1			$\frac{10}{27}$	$-\frac{25}{54}$	$\frac{5}{54}$	$-\frac{5}{189}$	$\frac{5}{108}$	$\frac{1}{756}$	$\frac{5}{7}$	$-\frac{1}{4}$
2	1	$-\frac{4}{3}$	0			$\frac{2}{9}$	$\frac{5}{18}$	$\frac{1}{18}$	$\frac{16}{63}$	$\frac{1}{9}$	$\frac{5}{63}$		
0	0	$\frac{2}{3}$	1			$\frac{1}{135}$	$\frac{1}{27}$	$\frac{5}{27}$	$-\frac{128}{945}$	$-\frac{10}{27}$	$\frac{50}{189}$		

$27 \otimes 6$	6	$\overline{15}$	$\overline{24}$	$\overline{42}$	$\overline{60}$	$\overline{15}$	$\overline{15'}$	$\overline{24}$	$\overline{42}$	$\overline{60}$	$\overline{42}$	$\overline{60}$
$\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$
$1 \frac{1}{2} -\frac{4}{3} 0$	$\frac{2}{15}$	$\frac{1}{9}$	$\frac{128}{315}$	$\frac{1}{9}$	$\frac{5}{21}$							
$0 0 -\frac{1}{3} \frac{1}{2}$	$-\frac{1}{15}$	$-\frac{2}{9}$	$\frac{4}{315}$	$-\frac{2}{9}$	$\frac{10}{21}$							
$0 1 -\frac{1}{3} \frac{1}{2}$	$\frac{1}{15}$	$0$	$\frac{4}{35}$	$-\frac{1}{2}$	$-\frac{42}{42}$	$-\frac{1}{8}$	$-\frac{5}{24}$	$\frac{1}{14}$	$0$	$\frac{25}{42}$		
$-1 \frac{1}{2} \frac{2}{3} 1$	$-\frac{4}{45}$	$-\frac{8}{27}$	$\frac{361}{945}$	$\frac{2}{27}$	$-\frac{10}{63}$	$\frac{1}{54}$	$\frac{5}{18}$	$-\frac{8}{189}$	$-\frac{25}{54}$	$\frac{25}{126}$		
$-1 \frac{3}{2} \frac{2}{3} 1$	$\frac{4}{9}$	$-\frac{10}{27}$	$-\frac{16}{189}$	$\frac{5}{54}$	$\frac{1}{126}$	$\frac{25}{108}$	$\frac{5}{36}$	$\frac{100}{189}$	$-\frac{1}{27}$	$-\frac{4}{63}$	$-\frac{1}{2}$	$\frac{1}{2}$
$0 2 -\frac{1}{3} \frac{1}{2}$						$\frac{25}{72}$	$-\frac{5}{24}$	$\frac{25}{126}$	$-\frac{2}{9}$	$-\frac{1}{42}$	$\frac{1}{2}$	$\frac{1}{2}$
$1 \frac{3}{2} -\frac{4}{3} 0$						$\frac{5}{18}$	$\frac{1}{6}$	$\frac{10}{63}$	$\frac{5}{18}$	$\frac{5}{42}$		

$27 \otimes 6$	6	$\overline{24}$	$\overline{60}$	$\overline{15}$	$\overline{24}$	$\overline{42}$	$\overline{60}$	$\overline{15'}$	$\overline{42}$	$\overline{60}$	$\overline{24}$	$\overline{60}$	$\overline{42}$	$\overline{60}$	$\overline{60}$
$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$
0 0 0	1	1	1	1	1	1	2	2	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	1	
$0 0 -\frac{4}{3} 0$	$\frac{1}{15}$	$\frac{16}{35}$	$\frac{10}{21}$												
$-1 \frac{1}{2} -\frac{1}{3} \frac{1}{2}$	$\frac{4}{15}$	$\frac{9}{35}$	$-\frac{10}{21}$	$-\frac{4}{27}$	$\frac{1}{189}$	$-\frac{10}{27}$	$\frac{10}{21}$								
$-2 1 \frac{2}{3} 1$	$\frac{2}{3}$	$-\frac{2}{7}$	$\frac{1}{21}$	$-\frac{5}{9}$	$\frac{20}{63}$	$\frac{1}{18}$	$-\frac{1}{14}$	$\frac{1}{3}$	$-\frac{1}{2}$	$\frac{1}{6}$					
$-1 \frac{3}{2} -\frac{1}{3} \frac{1}{2}$	$\frac{5}{27}$	$\frac{80}{189}$	$-\frac{8}{27}$	$-\frac{2}{21}$		$-\frac{1}{3}$	0	$\frac{2}{3}$							
0 1 $-\frac{4}{3} 0$	$\frac{1}{9}$	$\frac{16}{63}$	$\frac{5}{18}$	$\frac{5}{14}$											
0 2 $-\frac{4}{3} 0$						$\frac{1}{3}$	$\frac{1}{2}$	$\frac{1}{6}$							
$-1 \frac{1}{2} -\frac{4}{3} 0$						$\frac{2}{7}$	$\frac{5}{7}$								
$-2 1 -\frac{1}{3} \frac{1}{2}$						$\frac{5}{7}$	$-\frac{2}{7}$	$-\frac{1}{2}$	$\frac{1}{2}$						
$-1 \frac{3}{2} -\frac{4}{3} 0$						$\frac{1}{2}$	$\frac{1}{2}$								1
$-2 1 -\frac{4}{3} 0$															

Table 41: Isoscalar factors for  $28 \otimes 3$ .

$28 \otimes 3$	48	36	48	48	36	48	48	36
	$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
	$\frac{5}{2}$	$\frac{7}{2}$	2	3	3	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$
2 3 $\frac{1}{3} \frac{1}{2}$	-1	1						
1 $\frac{5}{2} \frac{1}{3} \frac{1}{2}$			-1	$-\frac{1}{7}$	$\frac{6}{7}$			
2 3 $-\frac{2}{3} 0$				$\frac{6}{7}$	$\frac{1}{7}$			
0 2 $\frac{1}{3} \frac{1}{2}$					-1	$-\frac{2}{7}$	$\frac{5}{7}$	
1 $\frac{5}{2} -\frac{2}{3} 0$						$\frac{5}{7}$	$\frac{2}{7}$	

$28 \otimes 3$	48 48 36 48 48 36 48 48 36 48 36 36 36
-2/3 -2/3 -2/3 -5/3 -5/3 -5/3 -8/3 -8/3 -8/3 -11/3 -11/3 -11/3 -14/3	
1 2 2 1/2 3/2 3/2 0 1 1 1/2 1/2 0	
-1 3/2 1/3 1/2	-1   -3/7 4/7
0 2 -2/3 0	4/7 3/7
-2 1 1/3 1/2	
-1 3/2 -2/3 0	
-3 1/2 1/3 1/2	
-2 1 -2/3 0	
-3 1/2 -2/3 0	
-4 0 1/3 1/2	
-4 0 -2/3 0	
	1

Table 42: Isoscalar factors for  $28 \otimes \bar{3}$ .

$28 \otimes \bar{3}$	63 21 63 63 21 63 63
8/3 5/3 5/3 5/3 2/3 2/3 2/3	
3 5/2 5/2 7/2 2 2 3	
2 3 2/3 0	1
1 5/2 2/3 0	-1/8 7/8
2 3 -1/3 1/2	7/8 1/8 1
0 2 2/3 0	-1/4 3/4
1 5/2 -1/3 1/2	3/4 1/4 1

$28 \otimes \bar{3}$	21 63 63 21 63 63 21 63 63 21 63 63 63
-1/3 -1/3 -1/3 -4/3 -4/3 -4/3 -7/3 -7/3 -7/3 -10/3 -10/3 -10/3 -13/3	
3/2 3/2 5/2 1 1 2 1/2 1/2 3/2 0 0 1 1/2	
-1 3/2 2/3 0	-3/8 5/8
0 2 -1/3 1/2	5/8 3/8 1
-2 1 2/3 0	
-1 3/2 -1/3 1/2	
-3 1/2 2/3 0	
-2 1 -1/3 1/2	
-4 0 2/3 0	
-3 1/2 -1/3 1/2	
-4 0 -1/3 1/2	
	1

Table 43: Isoscalar factors for  $\mathbf{28} \otimes \mathbf{6}$ .

$\mathbf{28} \otimes \mathbf{6}$			$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	
			$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
			2	3	4	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{7}{2}$	$\frac{7}{2}$	1	2	2	3	3	3	
2	3	$\frac{2}{3}$	1	1	-1	1											
1	$\frac{5}{2}$	$\frac{2}{3}$	1				1	$\frac{1}{6}$	$-\frac{5}{6}$	$-\frac{1}{4}$	$\frac{3}{4}$						
2	3	$-\frac{1}{3}$	$\frac{1}{2}$					$-\frac{5}{6}$	$-\frac{1}{6}$	$\frac{3}{4}$	$\frac{1}{4}$						
0	2	$\frac{2}{3}$	1									1	$\frac{1}{3}$	$-\frac{2}{3}$	$\frac{1}{21}$	$-\frac{5}{12}$	$\frac{15}{28}$
1	$\frac{5}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$									$-\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{5}{21}$	$\frac{1}{3}$	$\frac{3}{7}$	
2	3	$-\frac{4}{3}$	0										$\frac{5}{7}$	$\frac{1}{4}$	$\frac{1}{28}$		
$\mathbf{28} \otimes \mathbf{6}$			$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$			
			$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$								
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	0	1	1	2	2	2	2		
-1	$\frac{3}{2}$	$\frac{2}{3}$	1	1	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{7}$	$-\frac{1}{2}$	$\frac{5}{14}$								
0	2	$-\frac{1}{3}$	$\frac{1}{2}$		$-\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{8}{21}$	$\frac{1}{12}$	$\frac{15}{28}$								
1	$\frac{5}{2}$	$-\frac{4}{3}$	0				$\frac{10}{21}$	$\frac{5}{12}$	$\frac{3}{28}$								
-2	1	$\frac{2}{3}$	1							1	$\frac{2}{3}$	$-\frac{1}{3}$	$\frac{2}{7}$	$-\frac{1}{2}$	$\frac{3}{14}$		
-1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$							$-\frac{1}{3}$	$-\frac{2}{3}$	$-\frac{3}{7}$	0	$\frac{4}{7}$			
0	2	$-\frac{4}{3}$	0									$\frac{2}{7}$	$\frac{1}{2}$	$\frac{3}{14}$			
$\mathbf{28} \otimes \mathbf{6}$			$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{45}}$	$\overline{\mathbf{45}}$			
			$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{13}{3}$	$-\frac{13}{3}$	$-\frac{13}{3}$	$-\frac{16}{3}$		
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	1	1	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0		
-2	1	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{1}{6}$	$-\frac{5}{6}$	$-\frac{8}{21}$	$-\frac{1}{12}$	$\frac{15}{28}$									
-3	$\frac{1}{2}$	$\frac{2}{3}$	1	$\frac{5}{6}$	$-\frac{1}{6}$	$\frac{10}{21}$	$-\frac{5}{12}$	$\frac{3}{28}$									
-1	$\frac{3}{2}$	$-\frac{4}{3}$	0			$\frac{1}{7}$	$\frac{1}{2}$	$\frac{5}{14}$									
-3	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$						1	$-\frac{5}{21}$	$-\frac{1}{3}$	$\frac{3}{7}$					
-2	1	$-\frac{4}{3}$	0							$\frac{1}{21}$	$\frac{5}{12}$	$\frac{15}{28}$					
-4	0	$\frac{2}{3}$	1							$\frac{5}{7}$	$-\frac{1}{4}$	$\frac{1}{28}$					
-3	$\frac{1}{2}$	$-\frac{4}{3}$	0									$\frac{1}{4}$	$\frac{3}{4}$				
-4	0	$-\frac{1}{3}$	$\frac{1}{2}$							$-\frac{3}{4}$	$\frac{1}{4}$						
-4	0	$-\frac{4}{3}$	0													1	

Table 44: Isoscalar factors for  $\mathbf{35} \otimes \mathbf{3}$ .

$\mathbf{35} \otimes \mathbf{3}$			42	48	42	15'	42	48	48	42	15'	42	48	42	48
			$\frac{7}{3}$	$\frac{7}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{4}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{5}{2}$	
$\frac{3}{2}$	$\frac{5}{2}$	1	2	2	2	3	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	
2	2	$\frac{1}{3}$	$\frac{1}{2}$	-1	1										
1	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$			-1	$-\frac{2}{35}$	$-\frac{3}{25}$	$\frac{144}{175}$						
2	2	$-\frac{2}{3}$	0				$\frac{3}{7}$	$\frac{2}{5}$	$\frac{6}{35}$						
1	$\frac{5}{2}$	$\frac{1}{3}$	$\frac{1}{2}$				$\frac{18}{35}$	$-\frac{12}{25}$	$-\frac{1}{175}$	1					
0	1	$\frac{1}{3}$	$\frac{1}{2}$							-1	$-\frac{3}{28}$	$-\frac{1}{4}$	$\frac{9}{14}$		
1	$\frac{3}{2}$	$-\frac{2}{3}$	0								$\frac{5}{14}$	$\frac{3}{10}$	$\frac{12}{35}$		
0	2	$\frac{1}{3}$	$\frac{1}{2}$								$\frac{15}{28}$	$-\frac{9}{20}$	$-\frac{1}{70}$	$-\frac{1}{5}$	$\frac{4}{5}$
1	$\frac{5}{2}$	$-\frac{2}{3}$	0									$\frac{4}{5}$	$\frac{1}{5}$		

$\mathbf{35} \otimes \mathbf{3}$			42	15'	42	48	42	48	15'	42	48	42	15'	48	42	48	48
			$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{2}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{5}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{8}{3}$	$-\frac{11}{3}$
			0	1	1	1	2	2	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0	0	1	1	$\frac{1}{2}$
-1	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$	-1	$-\frac{1}{7}$	$-\frac{2}{5}$	$\frac{16}{35}$										
0	1	$-\frac{2}{3}$	0		$\frac{2}{7}$	$\frac{1}{5}$	$\frac{18}{35}$										
-1	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{2}$		$\frac{4}{7}$	$-\frac{2}{5}$	$-\frac{1}{35}$	$-\frac{2}{5}$	$\frac{3}{5}$								
0	2	$-\frac{2}{3}$	0					$\frac{3}{5}$	$\frac{2}{5}$								
-1	$\frac{1}{2}$	$-\frac{2}{3}$	0					$\frac{3}{14}$	$\frac{1}{10}$	$\frac{24}{35}$							
-2	0	$\frac{1}{3}$	$\frac{1}{2}$					$-\frac{1}{7}$	$-\frac{3}{5}$	$\frac{9}{35}$							
-2	1	$\frac{1}{3}$	$\frac{1}{2}$					$\frac{9}{14}$	$-\frac{3}{10}$	$-\frac{2}{35}$	$-\frac{3}{5}$	$\frac{2}{5}$					
-1	$\frac{3}{2}$	$-\frac{2}{3}$	0								$\frac{2}{5}$	$\frac{3}{5}$					
-2	0	$-\frac{2}{3}$	0								$\frac{1}{7}$	$\frac{6}{7}$					
-3	$\frac{1}{2}$	$\frac{1}{3}$	$\frac{1}{2}$								$\frac{6}{7}$	$-\frac{1}{7}$	$-\frac{4}{5}$	$\frac{1}{5}$			
-2	1	$-\frac{2}{3}$	0									$\frac{1}{5}$	$\frac{4}{5}$				
-3	$\frac{1}{2}$	$-\frac{2}{3}$	0													1	

Table 45: Isoscalar factors for  $\mathbf{35} \otimes \overline{\mathbf{3}}$ .

$\mathbf{35} \otimes \overline{\mathbf{3}}$			$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$
$\frac{8}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$							
2	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	1	1	2	2	2	2	2	2	3
2	2	$\frac{2}{3}$	0	1									
1	$\frac{3}{2}$	$\frac{2}{3}$	0		$-\frac{1}{7}$	$\frac{6}{7}$							
2	2	$-\frac{1}{3}$	$\frac{1}{2}$		$\frac{6}{7}$	$\frac{1}{7}$	$-\frac{1}{2}$	$\frac{1}{2}$					
1	$\frac{5}{2}$	$\frac{2}{3}$	0				$\frac{1}{2}$	$\frac{1}{2}$					
0	1	$\frac{2}{3}$	0						$-\frac{2}{7}$	$\frac{5}{7}$			
1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$						$\frac{5}{7}$	$\frac{2}{7}$	$\frac{1}{175}$	$-\frac{12}{25}$	$\frac{18}{35}$
0	2	$\frac{2}{3}$	0								$-\frac{6}{35}$	$\frac{2}{5}$	$\frac{3}{7}$
1	$\frac{5}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$								$\frac{144}{175}$	$\frac{3}{25}$	$\frac{2}{35}$
													1

$\mathbf{35} \otimes \overline{\mathbf{3}}$			$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$
$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{4}{3}$							
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	0	0	0	1	1	1	1	2
-1	$\frac{1}{2}$	$\frac{2}{3}$	0	$-\frac{3}{7}$	$\frac{4}{7}$									
0	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{4}{7}$	$\frac{3}{7}$	$\frac{1}{70}$	$-\frac{9}{20}$	$\frac{15}{28}$						
-1	$\frac{3}{2}$	$\frac{2}{3}$	0			$-\frac{12}{35}$	$\frac{3}{10}$	$\frac{5}{14}$						
0	2	$-\frac{1}{3}$	$\frac{1}{2}$			$\frac{9}{14}$	$\frac{1}{4}$	$\frac{3}{28}$	1					
-2	0	$\frac{2}{3}$	0						$-\frac{4}{7}$	$\frac{3}{7}$				
-1	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$						$\frac{3}{7}$	$\frac{4}{7}$	$\frac{1}{35}$	$-\frac{2}{5}$	$\frac{4}{7}$	
-2	1	$\frac{2}{3}$	0								$-\frac{18}{35}$	$\frac{1}{5}$	$\frac{2}{7}$	
-1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$								$\frac{16}{35}$	$\frac{2}{5}$	$\frac{1}{7}$	1

$\mathbf{35} \otimes \overline{\mathbf{3}}$			$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$
			$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	0	1
-2	0	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{35}$	$-\frac{3}{10}$	$\frac{9}{14}$		
-3	$\frac{1}{2}$	$\frac{2}{3}$	0	$-\frac{24}{35}$	$\frac{1}{10}$	$\frac{3}{14}$		
-2	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{9}{35}$	$\frac{3}{5}$	$\frac{1}{7}$	1	
-3	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$					1
								1

Table 46: Isoscalar factors for  $\mathbf{35} \otimes \mathbf{6}$ .

$\mathbf{35} \otimes \mathbf{6}$			$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{63}}$
			$\frac{8}{3}$	$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$							
2	2	$\frac{2}{3}$	1	1	-1	1							
1	$\frac{3}{2}$	$\frac{2}{3}$	1				1	$\frac{1}{35}$	$\frac{1}{5}$	$-\frac{27}{35}$	$-\frac{1}{10}$	$-\frac{1}{5}$	$\frac{7}{10}$
2	2	$-\frac{1}{3}$	$\frac{1}{2}$					$-\frac{2}{7}$	$-\frac{1}{2}$	$-\frac{3}{14}$	$\frac{3}{8}$	$\frac{1}{3}$	$\frac{7}{24}$
1	$\frac{5}{2}$	$\frac{2}{3}$	1					$-\frac{24}{35}$	$\frac{3}{10}$	$\frac{1}{70}$	$\frac{21}{40}$	$-\frac{7}{15}$	$-\frac{1}{120}$
													1

  

$\mathbf{35} \otimes \mathbf{6}$			$\overline{\mathbf{42}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$
			$\frac{2}{3}$										
0	1	$\frac{2}{3}$	1	1	1	1	2	2	2	2	2	3	3
1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$										
0	2	$\frac{2}{3}$	1										
1	$\frac{5}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$										
2	2	$-\frac{4}{3}$	0										

  

$\mathbf{35} \otimes \mathbf{6}$			$\overline{\mathbf{24}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{24}}$	$\overline{\mathbf{21}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$	$\overline{\mathbf{42}}$	$\overline{\mathbf{60}}$	$\overline{\mathbf{63}}$
			$-\frac{1}{3}$										
1	$\frac{3}{2}$	$-\frac{4}{3}$	0										
-1	$\frac{1}{2}$	$\frac{2}{3}$	1										
0	1	$-\frac{1}{3}$	$\frac{1}{2}$										
-1	$\frac{3}{2}$	$\frac{2}{3}$	1										
0	2	$-\frac{1}{3}$	$\frac{1}{2}$										
1	$\frac{5}{2}$	$-\frac{4}{3}$	0										

$35 \otimes 6$			$\overline{24}$	$\overline{60}$	$\overline{24}$	$\overline{21}$	$\overline{42}$	$\overline{60}$	$\overline{63}$	$\overline{42}$	$\overline{60}$	$\overline{63}$
			$-\frac{4}{3}$	$-\frac{4}{2}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$	$-\frac{4}{3}$
			0	0	1	1	1	1	1	1	2	2
0	1	$-\frac{4}{3}$	0		$\frac{16}{105}$	$\frac{3}{10}$	$\frac{1}{30}$	$\frac{3}{14}$	$\frac{3}{10}$			
-2	0	$\frac{2}{3}$	1		$\frac{4}{35}$	$-\frac{1}{10}$	$\frac{2}{5}$	$-\frac{2}{7}$	$\frac{1}{10}$			
-1	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$		$-\frac{5}{21}$	0	$-\frac{2}{15}$	$-\frac{2}{21}$	$\frac{8}{15}$			
-2	1	$\frac{2}{3}$	1		$-\frac{12}{35}$	$\frac{3}{10}$	$\frac{3}{10}$	$-\frac{1}{42}$	$-\frac{1}{30}$	$\frac{3}{10}$	$-\frac{1}{2}$	$\frac{1}{5}$
-1	$\frac{3}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$		$\frac{16}{105}$	$\frac{3}{10}$	$-\frac{2}{15}$	$-\frac{8}{21}$	$-\frac{1}{30}$	$-\frac{2}{5}$	0	$\frac{3}{5}$
0	2	$-\frac{4}{3}$	0							$\frac{3}{10}$	$\frac{1}{2}$	$\frac{1}{5}$

$35 \otimes 6$			$\overline{24}$	$\overline{21}$	$\overline{60}$	$\overline{63}$	$\overline{42}$	$\overline{60}$	$\overline{63}$	$\overline{21}$	$\overline{63}$	$\overline{60}$	$\overline{63}$	$\overline{63}$
			$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{7}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{10}{3}$	$-\frac{13}{3}$
			$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	$\frac{3}{2}$	0	0	1	1	$\frac{1}{2}$
-1	$\frac{1}{2}$	$-\frac{4}{3}$	0	$\frac{2}{35}$	$\frac{3}{10}$	$\frac{1}{7}$	$\frac{1}{2}$							
-2	0	$-\frac{1}{3}$	$\frac{1}{2}$	$-\frac{6}{35}$	$-\frac{1}{40}$	$-\frac{3}{7}$	$\frac{3}{8}$							
-2	1	$-\frac{1}{3}$	$\frac{1}{2}$	$\frac{3}{35}$	$\frac{9}{20}$	$-\frac{8}{21}$	$-\frac{1}{12}$	$-\frac{3}{10}$	$\frac{1}{6}$	$\frac{8}{15}$				
-3	$\frac{1}{2}$	$\frac{2}{3}$	1	$-\frac{24}{35}$	$\frac{9}{40}$	$\frac{1}{21}$	$-\frac{1}{24}$	$\frac{3}{5}$	$-\frac{1}{3}$	$\frac{1}{15}$				
-1	$\frac{3}{2}$	$-\frac{4}{3}$	0					$\frac{1}{10}$	$\frac{1}{2}$	$\frac{2}{5}$				
-2	0	$-\frac{4}{3}$	0					$\frac{1}{4}$	$\frac{3}{4}$					
-3	$\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{2}$					$\frac{3}{4}$	$-\frac{1}{4}$	$-\frac{2}{3}$	$\frac{1}{3}$			
-2	1	$-\frac{4}{3}$	0					$\frac{1}{3}$	$\frac{2}{3}$					
-3	$\frac{1}{2}$	$-\frac{4}{3}$	0											1

Table 47: Isoscalar factors for  $36 \otimes 3$ .

$36 \otimes 3$			$\overline{63}$	$\overline{45}$	$\overline{63}$	$\overline{63}$	$\overline{45}$	$\overline{63}$	$\overline{63}$	$\overline{45}$	$\overline{63}$	$\overline{63}$	$\overline{45}$
			$\frac{8}{3}$	$\frac{8}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{5}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
			3	4	$\frac{5}{2}$	$\frac{7}{2}$	$\frac{7}{2}$	2	3	3	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{5}{2}$
$\frac{7}{3}$	$\frac{7}{2}$	$\frac{1}{3}$	$\frac{1}{2}$	-1	1								
$\frac{4}{3}$	3	$\frac{1}{3}$	$\frac{1}{2}$			-1	$-\frac{1}{8}$	$\frac{7}{8}$					
$\frac{7}{3}$	$\frac{7}{2}$	$-\frac{2}{3}$	0			$\frac{7}{8}$	$\frac{1}{8}$						
$\frac{1}{3}$	$\frac{5}{2}$	$\frac{1}{3}$	$\frac{1}{2}$					-1	$-\frac{1}{4}$	$\frac{3}{4}$			
$\frac{4}{3}$	3	$-\frac{2}{3}$	0					$\frac{3}{4}$	$\frac{1}{4}$				
$-\frac{2}{3}$	2	$\frac{1}{3}$	$\frac{1}{2}$						-1	$-\frac{3}{8}$	$\frac{5}{8}$		
$\frac{1}{3}$	$\frac{5}{2}$	$-\frac{2}{3}$	0							$\frac{5}{8}$	$\frac{3}{8}$		

$\mathbf{36} \otimes \mathbf{3}$	$\overline{\mathbf{63}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{45}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{45}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{45}} \quad \overline{\mathbf{63}} \quad \overline{\mathbf{45}} \quad \overline{\mathbf{45}}$										
$-\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{4}{3} \quad -\frac{7}{3} \quad -\frac{7}{3} \quad -\frac{7}{3} \quad -\frac{10}{3} \quad -\frac{10}{3} \quad -\frac{10}{3} \quad -\frac{13}{3} \quad -\frac{13}{3} \quad -\frac{16}{3}$											
1      2      2 $\frac{1}{2}$ $\frac{3}{2}$ $\frac{3}{2}$ 0      1      1 $\frac{1}{2}$ $\frac{1}{2}$ 0											
$-\frac{5}{3} \quad \frac{3}{2} \quad \frac{1}{3} \quad \frac{1}{2}$	-1	$-\frac{1}{2} \quad \frac{1}{2}$									
$-\frac{2}{3} \quad 2 \quad -\frac{2}{3} \quad 0$		$\frac{1}{2} \quad \frac{1}{2}$									
$-\frac{8}{3} \quad 1 \quad \frac{1}{3} \quad \frac{1}{2}$			-1	$-\frac{5}{8} \quad \frac{3}{8}$							
$-\frac{5}{3} \quad \frac{3}{2} \quad -\frac{2}{3} \quad 0$				$\frac{3}{8} \quad \frac{5}{8}$							
$-\frac{11}{3} \quad \frac{1}{2} \quad \frac{1}{3} \quad \frac{1}{2}$					-1	$-\frac{3}{4} \quad \frac{1}{4}$					
$-\frac{8}{3} \quad 1 \quad -\frac{2}{3} \quad 0$						$\frac{1}{4} \quad \frac{3}{4}$					
$-\frac{11}{3} \quad \frac{1}{2} \quad -\frac{2}{3} \quad 0$							$\frac{1}{8} \quad \frac{7}{8}$				
$-\frac{14}{3} \quad 0 \quad \frac{1}{3} \quad \frac{1}{2}$							$-\frac{7}{8} \quad \frac{1}{8}$				
$-\frac{14}{3} \quad 0 \quad -\frac{2}{3} \quad 0$											1

Table 48: Isoscalar factors for  $\mathbf{36} \otimes \overline{\mathbf{3}}$ .

$\mathbf{36} \otimes \overline{\mathbf{3}}$	$80 \quad 28 \quad 80 \quad 80 \quad 28 \quad 80 \quad 80 \quad 28 \quad 80 \quad 80 \quad 80$										
3      2      2      2      1      1      1      0      0      0      0											
$\frac{7}{2} \quad 3 \quad 3 \quad 4 \quad \frac{5}{2} \quad \frac{5}{2} \quad \frac{7}{2} \quad 2 \quad 2 \quad 3$											
$\frac{7}{3} \quad \frac{7}{2} \quad \frac{2}{3} \quad 0$	1										
$\frac{4}{3} \quad 3 \quad \frac{2}{3} \quad 0$		$-\frac{1}{9} \quad \frac{8}{9}$									
$\frac{7}{3} \quad \frac{7}{2} \quad -\frac{1}{3} \quad \frac{1}{2}$		$\frac{8}{9} \quad \frac{1}{9}$	1								
$\frac{1}{3} \quad \frac{5}{2} \quad \frac{2}{3} \quad 0$				$-\frac{2}{9} \quad \frac{7}{9}$							
$\frac{4}{3} \quad 3 \quad -\frac{1}{3} \quad \frac{1}{2}$				$\frac{7}{9} \quad \frac{2}{9}$	1						
$-\frac{2}{3} \quad 2 \quad \frac{2}{3} \quad 0$						$-\frac{1}{3} \quad \frac{2}{3}$					
$\frac{1}{3} \quad \frac{5}{2} \quad -\frac{1}{3} \quad \frac{1}{2}$						$\frac{2}{3} \quad \frac{1}{3}$	1				

$36 \otimes \bar{3}$	28 80 80 28 80 80 28 80 80 28 80 80 80
	-1 -1 -1 -2 -2 -2 -3 -3 -3 -4 -4 -4 -5
	$\frac{3}{2} \frac{3}{2} \frac{5}{2} 1 1 2 \frac{1}{2} \frac{1}{2} \frac{3}{2} 0 0 1 \frac{1}{2}$
$-\frac{5}{3} \frac{3}{2} \frac{2}{3} 0$	$-\frac{4}{9} \frac{5}{9}$
$-\frac{2}{3} 2 -\frac{1}{3} \frac{1}{2}$	$\frac{5}{9} \frac{4}{9} 1$
$-\frac{8}{3} 1 \frac{2}{3} 0$	$-\frac{5}{9} \frac{4}{9}$
$-\frac{5}{3} \frac{3}{2} -\frac{1}{3} \frac{1}{2}$	$\frac{4}{9} \frac{5}{9} 1$
$-\frac{11}{3} \frac{1}{2} \frac{2}{3} 0$	$-\frac{2}{3} \frac{1}{3}$
$-\frac{8}{3} 1 -\frac{1}{3} \frac{1}{2}$	$\frac{1}{3} \frac{2}{3} 1$
$-\frac{14}{3} 0 \frac{2}{3} 0$	$-\frac{7}{9} \frac{2}{9}$
$-\frac{11}{3} \frac{1}{2} -\frac{1}{3} \frac{1}{2}$	$\frac{2}{9} \frac{7}{9} 1$
$-\frac{14}{3} 0 -\frac{1}{3} \frac{1}{2}$	1